



MORPHO MANUAL

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The Morpho system can be downloaded from
<http://morpho.cs.hi.is>.

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Abstract

Morpho is a multi-paradigm programming language that supports procedural, object-oriented and functional programming. Morpho has a unique module system that is designed to make it easy to compose modules in various ways. Module operations support generic programming by viewing modules as substitutions. The Morpho linker is an integral part of the Morpho compiler.

A major design goal in Morpho is to support ultra-lightweight threads and fibers. Morpho is stackless and has closures and lexical environments.

The Morpho runtime is implemented using a very simple scheme of indirect threading where each operation is an object. Morpho is implemented as a scripting language on top of Java. Morpho acts as a lightweight scripting language, adding scalability and functionality to Java.

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Part I
The Morpho Language

Chapter 1

Introduction

1.1 Installing Morpho

The Morpho system can be downloaded from the web¹. Follow the instructions on the web page.

1.2 Getting Started With Morpho

The basic Morpho system consists of the following parts:

- The file `morpho.jar` contains:
 - The Morpho compiler.
 - The Morpho runtime.
 - The Morpho basis module.
- The file `Morpho.pdf` contains the Morpho documentation.

In addition there is available a folder containing code examples and extra modules.

1.2.1 The Morpho Workbench

The Morpho workbench is a simple programming environment that supports a large subset of the Morpho programming language. The workbench makes it possible to program interactively in Morpho, but is not intended for creating Morpho modules or standalone Morpho executables.

¹<http://morpho.cs.hi.is>


```
1 "hello.mexe" = main in
2 {{
3 main =
4   fun()
5   {
6       writeln("Hello_world!");
7   };
8 }}
9 *
10 BASIS
11 ;
```

Figure 1.1: Hello World Program

To invoke the Morpho workbench you can use the following command on Windows, Linux or Macintosh:

```
java -jar morpho.jar
```

Or:

```
java -cp morpho.jar is.hi.cs.morpho.Morpho
```

Or, assuming that the proper bat-file or shell script has been set up, you can use the command:

```
morpho
```

On Windows, you can also use:

```
javaw -jar morpho.jar
```

Or:

```
javaw -cp morpho.jar is.hi.cs.morpho.Morpho
```

The Morpho workbench is largely self-explanatory once you start it.

1.2.2 A Simple Example

Figure 1.1 shows a simple stand-alone *hello world* program in Morpho. This is a program that is intended to be compiled and run from the command-line, not from inside the Morpho workbench.

We would type this program into a file named `hello.morpho` (or you could use any other file name if you wish). To compile the program you use the following command (assuming that your system contains the proper bat-file or shell script):

```
morpho -c hello.morpho
```

Or you can use the following command:

```
java -jar morpho.jar -c hello.morpho
```

Or:

```
java -cp morpho.jar is.hi.cs.morpho.Morpho -c hello.morpho
```

This will compile the program and create the file `hello.mexe`, which contains the executable version of the program. To run the program, we then use the command:

```
morpho hello
```

Or the following command:

```
java -jar morpho.jar hello
```

Or:

```
java -cp morpho.jar is.hi.cs.morpho.Morpho hello
```

That will cause the line

```
Hello world!
```

to be written to standard output, i.e. the computer screen.

This program consists of two modules, linked together using the importation module operation (denoted by `*`). One of the modules contains the function `main` and refers to the function `writeln`. The other module is the builtin module `BASIS`, which contains a variety of built-in functions, among them being the function `writeln`.

Figure 1.2 on the next page shows how the above program is linked. Further on in this manual we will see more module operations.

1.2.3 Another Example

The Morpho program in figure 1.3 on the following page is a little bit more complex.

As before, we might type this program into a file named `fibonacci.morpho`. To compile the program you could then use the command:

```
morpho -c fibonacci.morpho
```

This will compile the program and create the file `fibonacci.mexe`, and to run the program, we then use the command:

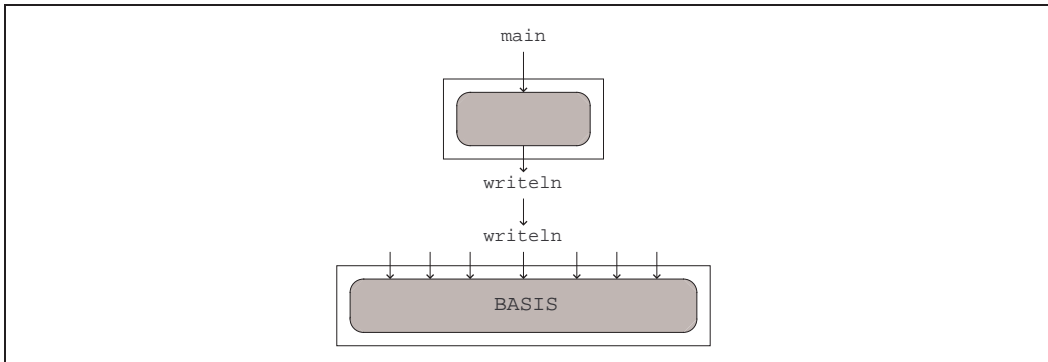


Figure 1.2: Linking A Simple Program

```

1 "fibo.mexe" = main in
2 {{
3 main =
4   fun()
5   {
6       writeln("fibo(10)="++fibo(10));
7   };
8 }}
9 *
10 !
11 {{
12 fibo =
13   fun(n)
14   {
15       if( n<=2 )
16       {
17           return 1;
18       }
19       else
20       {
21           return fibo(n-1)+fibo(n-2);
22       };
23   };
24 }}
25 *
26 BASIS
27 ;

```

Figure 1.3: Fibonacci Program

```
morpho fibo
```

That will cause the line

```
fibonacci(10)=55
```

to be written to standard output, i.e. the computer screen.

This program consists of three modules, linked together using a couple of different module operations, the importation module operation (denoted by `*`), and the iteration operation (a unary module operation denoted by `!`). One of the modules contains the function `main` and refers to the functions `writeln`, `++` and `fibonacci`. The other module is the builtin module `BASIS`, which contains a variety of built-in functions, among them being the functions `++`, `writeln`, `<=`, `-`, and `+`.

Figure 1.4 shows how the above program is linked. Remember that further on in this manual we will see more module operations.

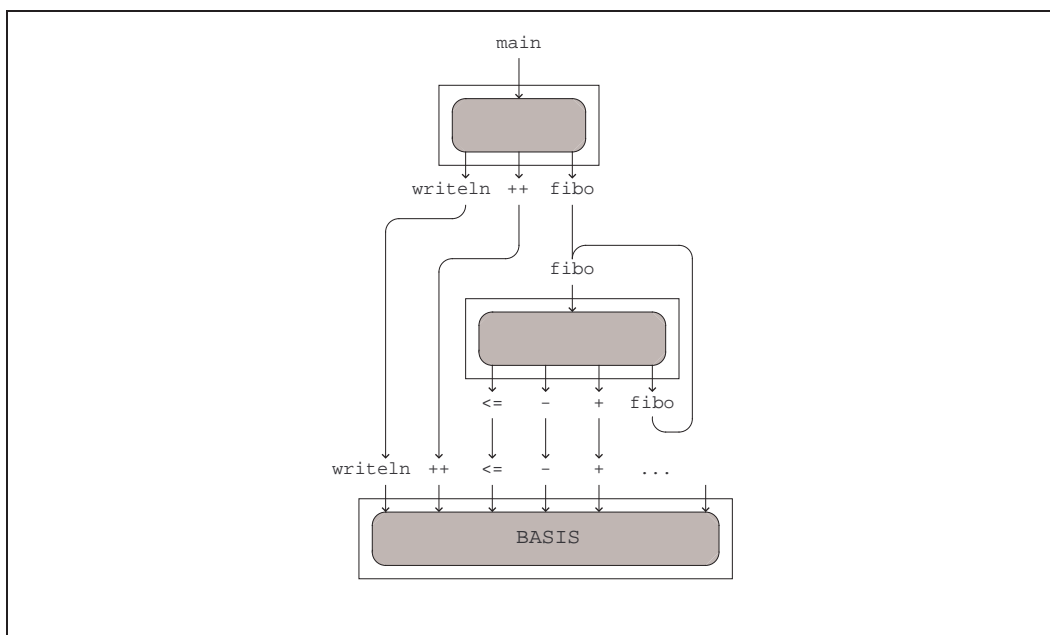


Figure 1.4: Linking The Fibonacci Program

Chapter 2

Expressions

Morpho has a wide variety of expression but no statements. Constructs such as if-then-else and while-do that are defined as statements in many other programming languages are expressions in Morpho.

2.1 Morpho Values

All values in Morpho are references to Java objects.¹

2.2 Literals

Literal expressions in Morpho evaluate to integers, doubles, characters, boolean values, strings, and the null reference. Evaluating a literal has no side effect.

2.2.1 Integer Literals

The syntax of integer literals is defined by syntax diagram 30 on page 48. Integer literals can be any number of digits. The value of an integer literal is a corresponding Java Integer object, a Java Long object or a Java BigInteger object. There is no limit on the size of an integer literal.

2.2.2 Double Literals

The syntax of double literals is defined by syntax diagram 32 on page 48. The value of a double literal is a corresponding Java Double object.

¹Future versions and variants of Morpho may run on top of other platforms than Java, in which case the Morpho values may be of other types. However, the basics of the Morpho language and the Morpho literal values will remain the same.

2.2.3 String Literals

The syntax of string literals is defined by syntax diagram 34 on page 49. The value of a string literal is a corresponding Java String object.

2.2.4 Character Literals

The syntax of character literals is defined by syntax diagram 33 on page 49. The value of a character literal is a corresponding Java Character object.

2.2.5 Boolean Literals

The literals `true` and `false` are boolean literals. The value of a boolean literal is a corresponding Java Boolean object.

2.2.6 The null Literal

The literal `null` is the null literal. Its value is the Java null reference.

2.3 Binary and Unary Operations

Unary and binary operations in Morpho are function calls to functions with one and two arguments, respectively.

The expression `'1+2'` is evaluated by calling the function `'+'` with arguments 1 and 2. Assuming that the function `'+'` is the usual addition function, the result will be the integer value 3.

Similarly, the expression `'"abc"++"def"'` is evaluated by calling the function `'++'`² with arguments `"abc"` and `"def"`, resulting in `"abcdef"`, assuming the usual meaning of the binary operator `'++'`.

The expression `'-(1-2)'` involves two different operations, the binary operation `'-'` and the unary operation `'-'`. The unary operation is, of course, a function of one argument. Note that the expressions `'-(1-2)'`, `'-1-2'`, `'-1-(2)'`, and `'-(1)-2'` all have different meanings because of operator precedence and also because `'-1'` is a single integer literal whereas `'-(1)'` is a unary operator applied to an integer literal.

²Note that the operator name `'++'` is a perfectly valid name of a binary operation. Similarly, you might think that `'1--2'` is equivalent to `'1-(-2)'`, but in fact that is not the case, `'1--2'` is an expression where the binary operator `'--'` is applied to two arguments, 1 and 2. For the expression `'1--2'` to work you would have to define the binary operator (function) `'--'`.

Precedence	First letter
7	'*', '/' or '%'
6	'+' or '-'
5	'<', '>', '!' or '='
4	'&' ¹
3	' ' ²
2	':'
1	'?', '~' or '^'

Table 2.1: Operator Precedence

2.3.1 Operator Precedence

Binary operators have various different precedences but all unary operators have the same precedence which is higher than that of binary operators.

The precedence of a binary operator depends on the first letter of the operator. Table 2.1 shows the various precedences. A higher precedence operator will be applied before a lower precedence operator, unless parentheses imply otherwise.

For example, the following expression pairs are equivalent:

- $1 * 2 + 3 * 4$ and $(1 * 2) + (3 * 4)$
- $1 + 2 < 3 * 4$ and $(1 + 2) < (3 * 4)$
- $1 < 2 \& 3 > 4$ and $(1 < 2) \& (3 > 4)$
- $1 \& 2 ? 3 | 4$ and $(1 \& 2) ? (3 | 4)$

2.3.2 Operator Associativity

Binary operators with precedence 2 (those starting with the letter ':') associate to the right. All others associate to the left.

For example, the following expression pairs are equivalent:

- $1 * 2 / 3 \% 4$ and $((1 * 2) / 3) \% 4$
- $1 + 2 - 3$ and $(1 + 2) - 3$
- $1 - 2 / 3 * 4 + 5$ and $(1 - ((2 / 3) * 4)) + 5$
- $1 : 2 : 3 + 4 + 5$ and $1 : (2 : ((3 + 4) + 5))$

¹Note that the '&&' binary operator has special handling and special precedence. See section 2.6.2 on page 18.

²Note that the '| |' binary operator has special handling and special precedence. See section 2.6.1 on page 18.

2.4 Variables

Morpho has a few different types of variables:

- Local variables and function parameters store information local to a particular function call.
- Global variables contain information that needs to be directly accessible in multiple parts of a system.
- Instance variable contain information local to a particular object instance.

Morpho supports pointers to variables (see 2.4.4 on page 16). It is possible to create a pointer to any type of variable and use that pointer to retrieve and change the value of the variable. Pointer arithmetic (as in C and C++) is not supported, nor is it possible to create pointers to array positions.

2.4.1 Local Variables And Parameters

The following declaration creates and defines variables, `x`, `y` and `z`.

```
var x=1 , y=x+1 , z ;
```

The variable `x` is initialized with the integer value 1 and `y` is initialized with the result of computing `x+1`. The variable `z` has no defined initial value.

The scope of a declaration such as the one above extends to the end of the enclosing block, i.e. from the preceding ‘{’ to the next enclosing ‘}’. We will later see more about such blocks.

We can also use the following declaration

```
val x=1 , y=x+1 ;
```

The difference between the first (**var**) version and the second (**val**) version is that the first one defines variables which can later receive new values in assignments such as

```
x=10 ;  
y=x+20 ;
```

whereas the second version defines “variables” (really constant values) which are not allowed to receive new values. Of course it makes no sense to define a **val** variable with no defined value so the following declaration is not allowed:

```
val z ;
```

2.4.2 Global Variables

There are three types of global variables: fiber variables, task variables and machine variables. They differ only in the way they interact with the parallel programming aspects of the Morpho language. Each Morpho fiber has a distinct copy of a fiber variable, but all fibers share the same copy of each task variable and machine variable. Each Morpho task has a distinct copy of each task variables, but all tasks share the same copy of each machine variable. Each machine can have multiple tasks and each task can have multiple fibers. On the other hand a task can only be associated with one machine and a fiber can only be associated with one task.

The following declaration declares one fiber variable, one task variable and one machine variable.

```
fibervar x;
taskvar y;
machinevar z;
```

A global variable must be declared in each scope it is used in. It is not possible to initialize global variables. They are automatically initialized with the **null** value when the corresponding machine, task or fiber is created.

2.4.3 Instance Variables And Morpho Objects

Morpho objects can contain instance variables. Each object (i.e. each instance of a "class") has it's own copy of each instance variable. Here's an example of a Morpho module containing a Morpho object definition, i.e. a constructor.

```
1 "complex.mmod" =
2 !
3 {{
4 ;;; Use:  z = makeComplex(x,y);
5 ;;; Pre:  x and y are real numbers.
6 ;;; Post: z is the complex number x+iy.
7 makeComplex =
8   obj(real,imag)
9   {
10    val x=real, y=imag;
11
12    ;;; Use:  a = z.x;
13    ;;; Pre:  z is a complex number.
14    ;;; Post: a is the real part of z.
15    msg get x
16    {
```

```
17     x;
18   };
19
20   ;;; Use: b = z.y;
21   ;;; Pre: z is a complex number.
22   ;;; Post: b is the imaginary part of z.
23   msg get y
24   {
25     y;
26   };
27
28   ;;; Use: z1 = z2.+z3;
29   ;;; Pre: z2 and z3 are complex numbers.
30   ;;; Post: z1 is the sum of z2 and z3.
31   msg +(z)
32   {
33     makeComplex(x+z.x,y+z.y);
34   };
35
36   ;;; Use: z1 = z2.-z3;
37   ;;; Pre: z2 and z3 are complex numbers.
38   ;;; Post: z1 is the difference of z2 and z3.
39   msg -(z)
40   {
41     makeComplex(x-z.x,y-z.y);
42   };
43
44   ;;; Use: z1 = z2.*z3;
45   ;;; Pre: z2 and z3 are complex numbers.
46   ;;; Post: z1 is the product of z2 and z3.
47   msg *(z)
48   {
49     makeComplex(x*z.x-y*z.y,x*z.y+y*z.x);
50   };
51
52   ;;; Use: z1 = z2./z3;
53   ;;; Pre: z2 and z3 are complex numbers.
54   ;;; Post: z1 is the quotient of z2 and z3.
55   msg /(z)
56   {
57     val d = z.x*z.x+z.y*z.y;
58     makeComplex((x*z.x+y*z.y)/d,(y*z.x-x*z.y)/d);
59   };
```

```

60     };
61   }}
62 ;

```

The definition

```
val x=real, y=imag;
```

defines two instance variables, `x` and `y`, which receive their values from the parameters `real` and `imag`. We could, instead, have defined the variables using the line

```
var x=real, y=imag;
```

which would have defined the same two variables as modifiable variables instead of as constants.

The instance variables of an object are only directly accessible inside methods for that object, such as the methods for the messages `+`, `-`, `*`, and `/`. But note that we can, if we wish, define accessor messages (and their corresponding methods) for each variable, such as the ones defined for `x` and `y` in the above example.

2.4.4 Pointers To Variables

Morpho supports pointers with semantics similar to that of C and C++. If `x` is a variable of any kind (local, instance, etc.) then the expression `&x` returns a pointer to that variable. If a variable `p` contains such a pointer then the expression `*p` refers to the variable `x` and can be used as an assignment target to give `x` a new value or it can be used to fetch the value of `x`.

For example, the following lines of code will print the value 123 twice.

```

1   var x, p;
2   p = &x;
3   x = 321;    ;;; Overridden by the next line
4   *p = 123;
5   writeln("x="++x);
6   *p = 321;    ;;; Overridden by the next line
7   x = 123;
8   writeln("x="++x);

```

In contrast to the semantics of C and C++, pointer values in Morpho will remain valid indefinitely. This means that variables referred to by pointers remain living while any such pointers refer to them. In particular, if a pointer is made to refer to a local variable in a function then that variable will exist after the call to the function has completed and until no pointers refer to it. Similarly, if a pointer

refers to an instance variable of an object, the object will remain in existence even if there are no other references to it.

Morpho does not support pointers to positions in arrays. Neither does it support pointer arithmetic.

2.5 Lists

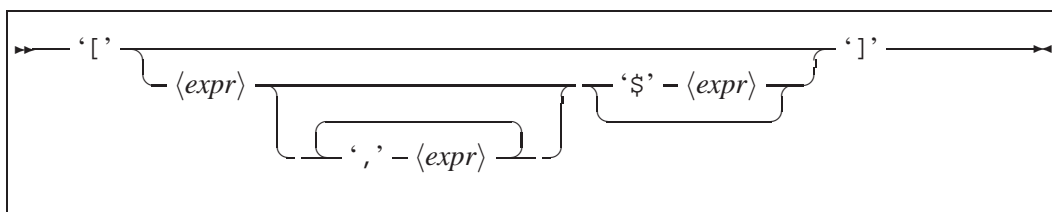
Morpho is, among other things, a list processing language. Morpho has built in syntax and functions to make list processing easier. Here's some example code that uses the list syntax and fundamental list functions to construct lists.

```

1  var x, y, z;
2  x = [1,2];           ;; Construct a list
3  y = 1:2:[];         ;; The same list again
4  z = [1$[2$[]]];     ;; And same again
5  writeln(head(x));   ;; Writes 1
6  writeln(head(tail(x))); ;; Writes 2

```

Syntax diagram 1 describes how to construct a list using Morpho syntax. The list syntax diagram is part of diagram 57 on page 61 for simple expressions.



Syntax Diagram 1: *<list>*

This list syntax is ‘syntactic sugar’, the same effects can be achieved by using the ‘:’ operation in the BASIS module. An expression $[x, \dots]$ is equivalent to the expression $x : [\dots]$ and an expression $[x\$y]$ is equivalent to $x : y$.

2.5.1 The Empty List

The expression $[\]$ is equivalent to the expression **null**. Both return the null reference.

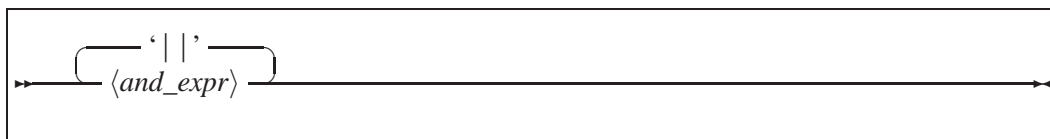
2.6 Logical Expressions

Morpho has logical operators $||$, $\&\&$ and $!$, standing for the logical operations ‘or’, ‘and’ and ‘not’. Contrary to all other operations in Morpho, these are built

into the language, and their semantics can not be modified. The binary logical operations have short-circuit semantics, as described below.

2.6.1 Or Expression

An or expression is a sequence of expressions separated by the operator ‘||’, as shown in diagram 2 (the same diagram as 52 on page 59). The effect of an

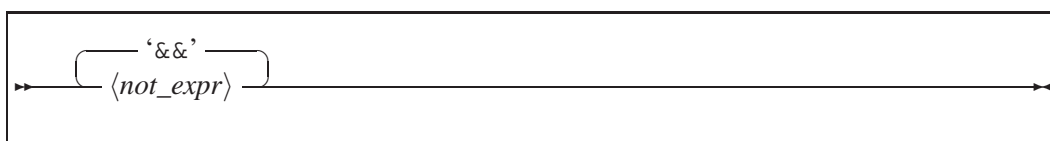


Syntax Diagram 2: $\langle or_expr \rangle$

expression $x \ || \ y$, where x and y are sub-expressions, is to evaluate x , check whether the result is true, and if so, return that result. If the result is false then y is evaluated and the resulting value is the value of the whole expression. It should be noted that the only false values are the null reference and the boolean false value (the results from the expressions **null** and **false**, respectively). A consequence of this definition is that the ‘||’ operator is associative, i.e. the expressions $x \ || \ (y \ || \ z)$ and $(x \ || \ y) \ || \ z$ are semantically equivalent.

2.6.2 And Expression

An and expression is a sequence of expressions separated by the operator ‘&&’, as shown in diagram 3 (the same diagram as 53 on page 59). The effect of an

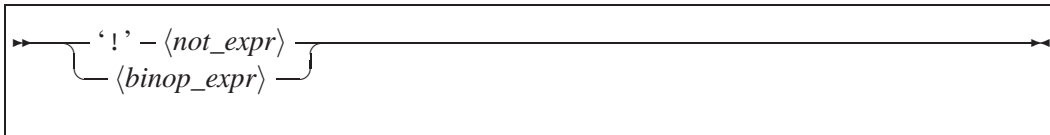


Syntax Diagram 3: $\langle and_expr \rangle$

expression $x \ \&\& \ y$, where x and y are sub-expressions, is to evaluate x , check whether the result is false, and if so, return that result. If the result is true then y is evaluated and the resulting value is the value of the whole expression. As with the or expression, a consequence of this definition is that the ‘&&’ operator is associative, i.e. the expressions $x \ \&\& \ (y \ \&\& \ z)$ and $(x \ \&\& \ y) \ \&\& \ z$ are semantically equivalent.

2.6.3 Not Expression

The built-in unary operator ‘!’ is the logical negation operator. Syntax diagram 4 (same as 54 on page 60) shows the pattern for not expressions. The expression

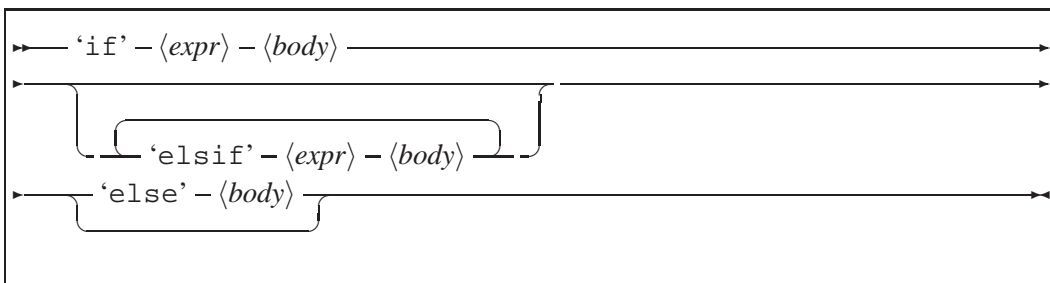


Syntax Diagram 4: $\langle not_expr \rangle$

!x returns **true** if x returns false and **false** if x returns true. The return value is always a boolean value but the argument to the operator can be any value. Remember that the only false values are **false** and **null**, so that **!null** as well as **!false** will return **true** whereas (for example) !0 and !"false" will return **false**.

2.7 The ‘if’ Expression

Syntax diagram 5 (same as diagram 63 on page 63) shows the pattern of the if expression in Morpho. The effect of a simple if expression



Syntax Diagram 5: $\langle if_expr \rangle$

```

1      if cond
2      {
3          body1;
4      }
5      else
6      {
7          body2;
8      }

```

is to evaluate the condition `cond` and then either evaluate `body1` or `body2`, depending on whether `cond` evaluated to true or false, respectively. An expression

```
if cond
{
    body1;
}
```

without any **else** part, is equivalent to

```
if cond
{
    body1;
}
else
{
    random;
}
```

where random is some undefined value.

An expression

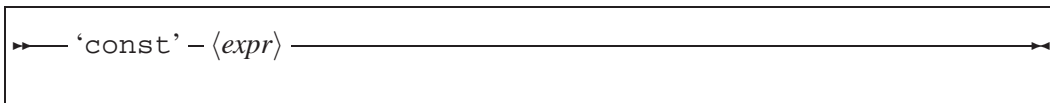
```
if cond1
{
    body1;
}
elsif cond2
...
```

is equivalent to

```
if cond1
{
    body1;
}
else
{
    if cond2
    ...;
}
```

2.8 The 'const' Expression

The const expression is used to compute a constant value that we don't want to recompute again. Diagram 6 on the following page (also part of diagram 51 on page 59) shows the pattern of the const expression. The effect of a const



Syntax Diagram 6: $\langle const_expr \rangle$

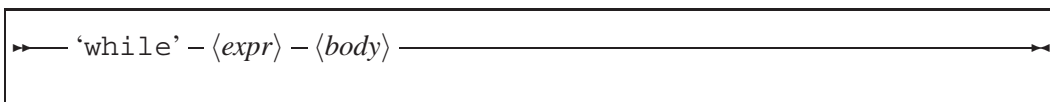
expression **const** e , when it is evaluated the first time, is to evaluate the sub-expression e , and return that value. The value is also saved so that the next time the same const expression is evaluated the old result is returned again.

2.9 Looping Expressions

Morpho has a couple of looping expressions; the while expression and the for expression.

2.9.1 The 'while' Expression

Syntax diagram 7 which part of syntax diagram 57 on page 61 defines pattern of the while expression. The effect of the while expression **while**(c) { x ; } is to



Syntax Diagram 7: $\langle if_expr \rangle$

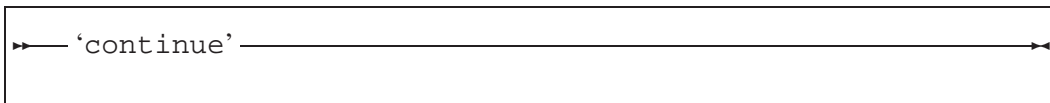
evaluate the condition c and then if the result is true evaluate the body { x ; }, after which the loop starts again. If the result of evaluating the condition c is false then the evaluation of the while expression terminates and the expression returns some undefined value (unless a break expression terminates the while expression, see section 2.9.3 on the following page).

2.9.2 The 'for' Expression

Syntax diagram 8 on the next page (same as diagram 62 on page 63) shows the syntax pattern of for expressions. The effect of a for expression of the form

```
for( init ; cond ; iter )
{
  body;
}
```

is as follows. First the expression `iter` is evaluated. This is done once at the beginning of the evaluation of the for expression. After that we enter a loop where



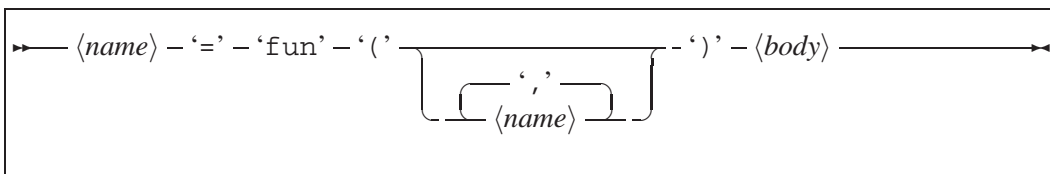
Syntax Diagram 10: $\langle \text{continue_expr} \rangle$

back to the beginning, i.e. to the evaluation of the condition at the beginning of the loop.

2.10 Function Definitions

2.10.1 Top-Level Functions

Diagram 11 shows how to define a top-level function that is exported from a module (see also diagram 46 on page 56 and diagram 44 on page 55). Here are a



Syntax Diagram 11: $\langle \text{top_fun_def} \rangle$

couple of simple function definitions inside a module.

```

1 "fibonacci.mmod" =
2 !
3 {{
4 fibo1 =
5   fun(n)
6   {
7     if( n<2 )
8     {
9       1;
10    }
11    else
12    {
13      fibo1(n-1)+fibo1(n-2);
14    };
15  };
16
17 fibo2 =
18   fun(n)
19   {

```

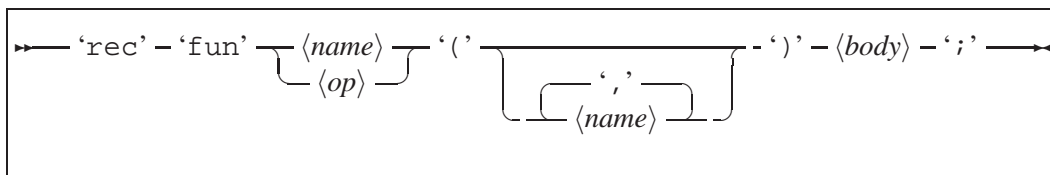
```

20  var i = 0, f1 = 1, f2 = 1;
21  while( i!=n )
22  {
23      val nextf = f1+f2;
24      i = inc(i);
25      f1 = f2;
26      f2 = nextf;
27  };
28  f1;
29  };
30  }}
31  ;

```

2.10.2 Inner Functions

Diagram 12 shows how to define a single inner function that can be defined inside another function or inside an object definition. See also diagram 50 on page 58 for a fuller syntax of recursive definitions in general. An inner function definition



Syntax Diagram 12: *<inner_fun_def>*

is a declaration and can be placed inside any body, including a function body or the bodies of compound expressions.

Here is an example of a simple function definition inside a Morpho program.

```

1  "fibonacci" = main in
2  {{
3  main =
4  fun()
5  {
6      rec fun fibo(n)
7      {
8          if( n<2 )
9          {
10             1;
11         }
12         else
13         {

```

```

14         fibol(n-1)+fibol(n-2);
15     };
16 };
17     writeln("fibol(10)="+++fibol(10));
18 };
19 }}
20 *
21 BASIS
22 ;

```

It is also possible to define anonymous functions as stand-alone expressions (see diagram 24 on page 42), and the values resulting from such expressions can be assigned to variables. Using this method we can do the following:

```

1 "fibol.mexe" = main in
2 {{
3 main =
4     fun()
5     {
6         rec val fibol =
7             fun(n)
8             {
9                 if n<2
10                {
11                    1;
12                }
13                else
14                {
15                    fibol(n-1)+fibol(n-2);
16                };
17            };
18     writeln("fibol(10)="+++fibol(10));
19 };
20 }}
21 *
22 BASIS
23 ;

```

This achieves the same effect as the previous example.

Note that it is possible to have multiple definitions of the same function. For example:

```

1 "fibol.mexe" = main in
2 !
3 {{

```

```
4 main =
5   fun()
6   {
7     rec val fibo =
8       fun(n)
9       {
10        if n<2
11        {
12          1;
13        }
14        else
15        {
16          fibo1(n-1)+fibo1(n-2);
17        };
18      };
19     rec fun fibo(n)
20     {
21       if n<2
22       {
23         1;
24       }
25       else
26       {
27         fibo1(n-1)+fibo1(n-2);
28       };
29     };
30     writeln("fibo(10)="+fibo(10));
31   };
32
33 fibo =
34   fun(n)
35   {
36     if n<2
37     {
38       return 1;
39     }
40     else
41     {
42       return fibo(n-1)+fibo(n-2);
43     };
44   };
45 }}
46 *
```

47 BASIS

48 ;

How then is each call to `fibonacci` resolved? The general answer is that first a search is made for an inner function definition (i.e. `rec fun . . .`) and if such a definition is found in the current scope or some enclosing scope, with the correct number of parameters, then that function definition is used. The innermost definition is used if there are multiple such definitions in enclosing scopes. If no such function definition is found, then a search is made for a variable in the current or enclosing scope that has the name `fibonacci`, or in the general case the name of the function being called. If such a variable is found then it is assumed that this variable contains a function value (also called a *closure*), and a call is made to the function value. If neither of the above cases apply then it is assumed that the function is a top-level function.

Similar rules apply to unary and binary operations, which can be either inner functions or top-level functions. They can not be variables, however, as there is no syntax to define variables with such names.

Mutual Recursion

Sometimes it is useful to define a collection of mutually recursive values, variable initializations and inner functions. The syntax and semantics of recursive definitions facilitates this. Note that inner function definitions are part of this syntax, see diagram 50 on page 58 for a fuller syntax of such definitions.

Here is an example of two mutually recursive functions. Note that the mutually recursive functions need to be defined in a single declaration.

```

1 "foo.mexe" = main in
2 {{
3 main =
4   fun()
5   {
6     rec
7     fun a(n)
8     {
9       if n==0 {return []};
10      write("a");
11      b(n-1);
12    },
13    fun b(n)
14    {
15      if n==0 {return []};
16      write("b");

```

```

17         a(n-1);
18     };
19     a(10);
20 };
21 }}
22 *
23 BASIS
24 ;

```

Here is another example with mutually referencing variables and values.

```

1 "foo.mexe" = main in
2 {{
3 main =
4   fun()
5   {
6     rec val a, var b=#[1$a], val a=#[2$b];
7     writeln(streamHead(a));
8     writeln(streamHead(b));
9     writeln(streamHead(streamTail(a)));
10    writeln(streamHead(streamTail(b)));
11  };
12 }}
13 *
14 BASIS
15 ;

```

This will write the integer sequence 2,1,1,2. Note that in order for it to be legal to reference a named value (such as `a` above) or a variable in the right hand side of an initialization, the named value or variable must have been defined before it is referenced. Furthermore, all declared named values must receive an initialization in the same declaration they are declared in.

In a recursive declaration the functions, named values and variables are first all created and then they are initialized in sequence.

2.10.3 The ‘return’ Expression

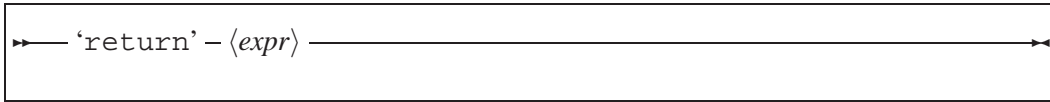
The return expression is used to terminate the current function call or method call. Diagram 13 on the next page shows the pattern of the return expression. See also diagram 51 on page 59.

The following program text does the same as the text above, but uses the return statement.

```

1 "fibonacci" =

```

Syntax Diagram 13: $\langle \text{return} \rangle$

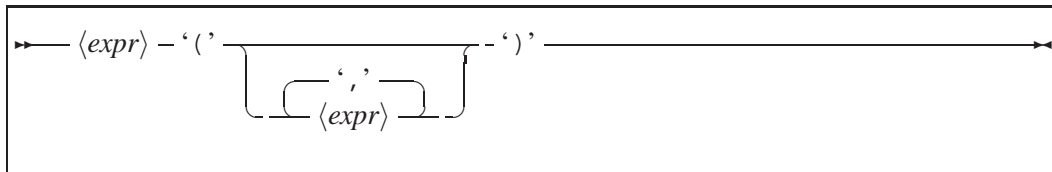
```

2 !
3 {{
4 fibo1 =
5   fun(n)
6   {
7     if( n<2 )
8     {
9       return 1;
10    }
11    else
12    {
13      return fibo1(n-1)+fibo1(n-2);
14    };
15  };
16
17 fibo2 =
18   fun(n)
19   {
20     var i = 0, f1 = 1, f2 = 1;
21     for(;;)
22     {
23       if( i==n )
24       {
25         return f1;
26       };
27       val nextf = f1+f2;
28       i = inc(i);
29       f1 = f2;
30       f2 = nextf;
31     };
32  };
33 }}
34 ;

```

2.11 Function Calls

Diagram 14 (which is essentially part of diagram 56 on page 60) shows the pattern of a function call in Morpho. The effect of a function call $e(e_1, \dots, e_N)$ is to

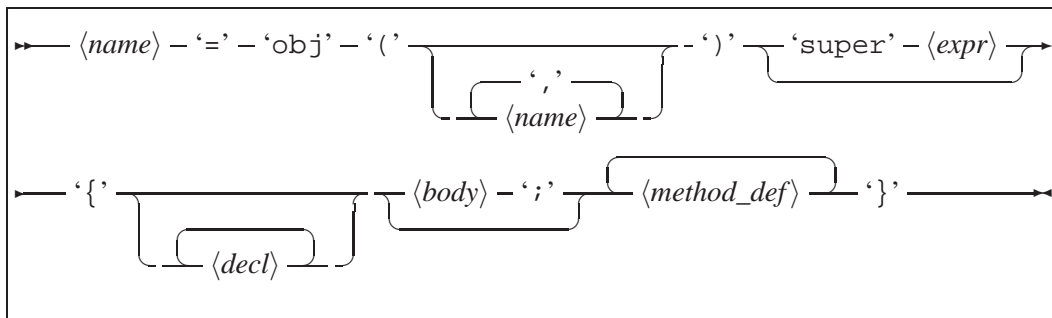


Syntax Diagram 14: $\langle \text{fun_expr} \rangle$

evaluate the expressions e, e_1, \dots, e_N , in order, and then make a call to the value returned by e (assuming e is a function, or, in other words, a closure, taking N arguments), with the results of e_1, \dots, e_N as arguments. If e is a name then the function to be called is resolved as described in section 2.10.2 on page 24, but in general e can be any expression.

2.12 Object Definitions

Diagram 15 (which includes diagram 47 on page 57) shows the pattern for defining a Morpho object or class. The following example shows a couple of object



Syntax Diagram 15: $\langle \text{obj_def} \rangle$

definitions in a module.

```

1 "objexample.mmod" =
2 !
3 {{
4 stack =
5   obj(max)
6   {
7     var arr = makeArray(max);

```

```
8     val limit = max;
9     var pos = 0;
10    msg push(x)
11    {
12        pos < limit ||
13        (throw "Attempt_to_push_on_a_full_stack");
14        arr[pos] = x;
15        pos = inc(pos);
16    };
17    msg pop()
18    {
19        pos > 0 ||
20        (throw "Attempt_to_pop_from_an_empty_stack");
21        pos = dec(pos);
22        return arr[pos];
23    };
24    msg isEmpty()
25    {
26        return (pos == 0);
27    };
28    msg isFull()
29    {
30        return (pos == limit);
31    };
32 };
33
34 extendedStackOfDouble =
35 obj() super stack()
36 {
37     var count = 0.0;
38     var sumx = 0.0;
39     var sumxx = 0.0;
40     msg push(x)
41     {
42         sumx = sumx + x;
43         sumxx = sumxx + x*x;
44         count = count + 1.0;
45         super.push(x);
46     };
47     msg pop()
48     {
49         val x = super.pop();
50         sumx = sumx - x;
```

```
51     sumxx = sumxx - x*x;
52     count = count - 1.0;
53     return x;
54 };
55 msg count()
56 {
57     return count;
58 };
59 msg average()
60 {
61     return sumx/count;
62 };
63 msg stdDev()
64 {
65     return
66         "java.lang.Math".##sqrt(
67             (sumxx-sumx*sumx/count)/count
68         );
69 };
70 };
71 }}
72 i
```

2.12.1 ‘this’ And ‘super’

There are two special expressions in Morpho that can only be used inside methods of objects. The expression this is used to refer to the current object. For example, inside a method, the expression this.f(1) is used to send the message f with the argument 1 to the current object. The method to be executed is determined by traversing the inheritance of the object, from the bottom to the top (the topmost ‘superclass’) and executing first method found that is associated with the message.

Sometimes, however, there is the need to send a message to the current object and make sure that the corresponding method to be executed is a method of a ‘superclass’ of the object rather than executing the first method in the inheritance path. In that case we use the special expression super, which is also only available inside methods. We see examples of this above in the methods for push and pop in the subclass extendedStackOfDouble.

2.13 Constructing Objects

An object is constructed by calling a constructor. Seen from the outside, a constructor is simply a function. The syntax of defining a constructor is different, however. Here are a couple of definitions, one is a constructor, the other one is a function.

```
1 "example.mmod" =
2 {{
3 f =
4   fun()
5   {
6     1;
7   };
8
9 g =
10  obj()
11  {
12    msg h()
13    {
14      2;
15    };
16  };
17 }}
18 ;
```

Seen from the outside both `f` and `g` are functions taking no arguments and returning some value. In the case of `f`, the value returned is the integer 1, whereas a call `g()` returns an object which responds to the message `h()` by returning the integer 2.

2.14 Scope of Declarations

We have seen various types of declarations, but they can be split into two major types; recursive declarations that start with the keyword ‘`rec`’ and non-recursive declarations that do not. Both these types of declarations can involve initializations, especially the recursive ones.

The scope of a name defined in a recursive declaration extends from the *beginning* of the declaration (i.e. just after the keyword ‘`rec`’ that starts the declaration) and to the end of the block that contains the declaration, i.e. up to the closing curly brace, ‘`}`’.

On the other hand the scope of a name defined in a non-recursive declaration extends from the *end* of the declaration and up to the end of the containing block.

Take for example the following program that demonstrates the difference between a recursive declaration and a non-recursive one in a simple way.

```

1 "example.mexe" = main in
2 {{
3 main =
4 fun()
5 {
6   val x=#[1];
7   {
8     val x=#[2$x];      ;;; x is #[2,1]
9     writeln(streamHead(streamTail(x)));
10    };
11    {
12     rec val x=#[2$x];   ;;; x is #[2,2,2,2,...]
13     writeln(streamHead(streamTail(x)));
14    };
15   };
16 }}
17 *
18 BASIS
19 ;

```

This program will write the two integers 1, 2.

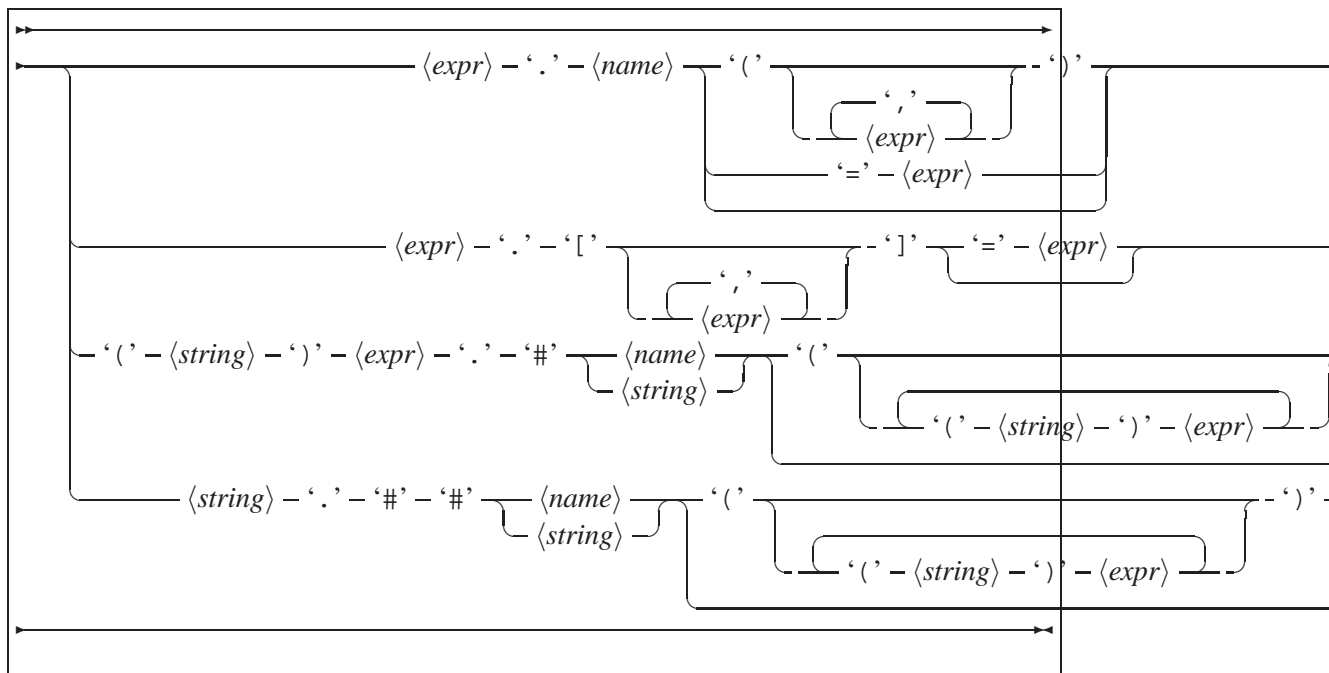
2.15 Method-Call Expressions

There are three types of method call expressions in Morpho. One is for sending a Morpho message to a Morpho object, one for sending a Java instance message to a Java object, and one is for sending a Java static class message to a Java class.

Diagram 16 on the following page shows the patterns of the possible method invocations in Morpho. This diagram, while correct, does not take into account the diverse precedences of Morpho constructs. See diagram 56 on page 60 and others below to see diagrams that take the syntactic precedence structure of Morpho into account.

2.15.1 Morpho Method Invocations

There are five patterns of Morpho method invocations.



Syntax Diagram 16: $\langle method_invokation \rangle$

- The effect of a regular Morpho method invocation such as $e.f(e_1, \dots, e_N)$ is to first evaluate the expression e , then evaluate the expressions e_1, \dots, e_N in sequence, and finally send the message f to the result from e with the results from e_1, \dots, e_N as arguments. The result from that invocation is then the result from evaluating the total expression.
- The effect of an accessor method invocation such as $e.x$ is to evaluate e and send the accessor message x to the result. The result from the method that the message invokes becomes the result of the whole expression.
- The effect of an accessor method invocation such as $e_1.x=e_2$ is to evaluate e_1 and e_2 , in that order, and send the accessor message $x=$ to the result from e_1 with the result from e_2 as argument. The result from the method that the message invokes becomes the result of the whole expression.
- The effect of a array accessor Morpho method invocation such as $e.[e_1, \dots, e_N]$ is to first evaluate the expression e , then evaluate the expressions e_1, \dots, e_N in sequence, and finally send the array accessor message to the result from e with the results from e_1, \dots, e_N as arguments. The result from that invocation is then the result from evaluating the total expression.
- The effect of a array assignment Morpho method invocation such as $e_0.[e_1, \dots, e_N]=e$ is to first evaluate the expression e_0 , then evaluate the

expressions e_1, \dots, e_N and e in sequence, and finally send the array assignment message to the result from e_0 with the results from e_1, \dots, e_N and e as arguments. The result from that invocation is then the result from evaluating the total expression.

2.15.2 Java Instance Method Invocations

Morpho supports invocations of Java instance methods through a special syntax. An expression $(t)e.\#f((t_1)e_1, \dots, (t_N)e_N)$ has the effect of first evaluating e and then evaluating e_1, \dots, e_N , in order, and then sending the Java message f to the result from e , with the results from e_1, \dots, e_N as arguments. The expressions t, t_1, \dots, t_N must be string literals and must be fully qualified class names. The message f is resolved at run-time on the basis of the number and types of the arguments t_1, \dots, t_N , and the type of the receiver of the message, t .

For example, imagine we have Java classes A and B where B is a subclass of A, as follows:

```

1 class A
2 {
3   A f( A x )
4   {
5     return x;
6   }
7 }
8
9 class B extends A
10 {
11   A f( A x )
12   {
13     return x;
14   }
15 }
```

Now assume that the Morpo variable x contains a reference to a Java object of class B. Then the invocation $("B")x.\#f(("B")x)$ will fail because the run-time system will try to find a method taking an argument of type B, which it won't find. In order to invoke the method you should specify the precise type of argument as declared in the class. The invocation $("A")x.\#f(("A")x)$ will succeed because it's effect is to look for a method named f which takes a single argument of type A and send x as that argument (x is, of course, both of type A and of type B because B is a subclass of A).

The following Morpo code is another example.

```
1 y = ("java.math.BigDecimal")y.#add(("java.math.BigDecimal")y);
```

Here the programmer specifies that y is of type `java.math.BigDecimal` and uses the Java instance method `add` to double its value.

2.15.3 Java Class Method Invocations

Java class methods can be invoked in Morpho using expressions such as $t.##f((t_1)e_1, \dots, (t_N)e_N)$ (note the double ‘#’, as opposed to the single ‘#’ used in instance method invocations). The expression t must be a string literal and must be the full name of a Java class. The same holds for t_1, \dots, t_N . f may be either a name or a string and should be the name of a static method in the class. The static class method denoted by f is invoked for the class denoted by t , with the arguments being the values yielded by e_1, \dots, e_N , which must be of types denoted by t_1, \dots, t_N . The order of evaluation of the expressions e_1, \dots, e_N is, as you would expect, from left to right.

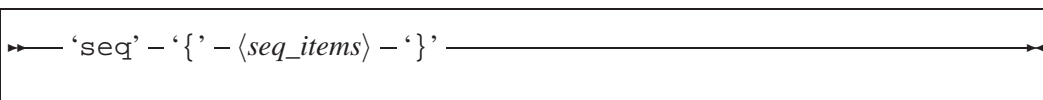
The following is an example of using a call to a static class method to compute pi.

```
1 val PI = "java.lang.Math".##atan2(("double")0.0, ("double")-1.0);
```

2.16 The ‘seq’ Expression

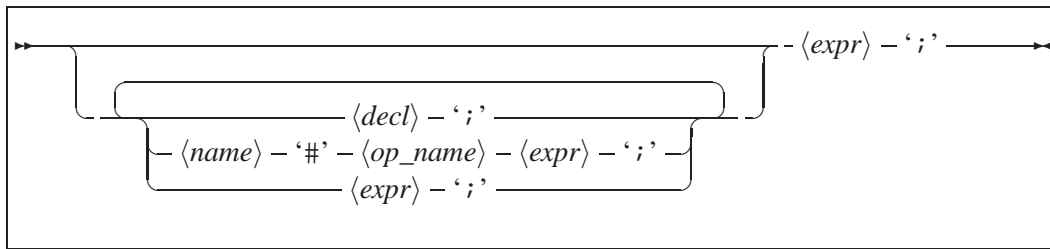
The purpose of the `seq` expression is to support a well-known style of functional programming where values from a container are fed through a kind of production line of functions where each function manipulates a value and produces values into another container. The `seq` expression is closely related to `do` expressions and list comprehensions in the functional programming language Haskell.

Syntax diagrams 17 (also part of 57 on page 61) and 18 on the following page (same as 61 on page 62) show the pattern of the ‘seq’ expression in Morpho.



Syntax Diagram 17: $\langle seq_expr \rangle$

The `seq` expressions are really just syntactic sugar, i.e. they are a little more convenient way of expressing things that can already be expressed in Morpho in other ways. Consequently, the semantics of a `seq` expression can be described by showing alternate ways of writing a semantically equivalent expression.



Syntax Diagram 18: $\langle seq_items \rangle$

- A seq expression **seq** { *expr*; } where *expr* is an expression is simply equivalent to the expression *expr*.
- A seq expression **seq** { *decl*; ... } where *decl* is a declaration is equivalent to the expression { *decl*; **seq** { ... }; }.
- And finally, and most important, a seq expression **seq** { *x* #<=<= *e*; ... } is equivalent to the binary function (operator) call *e* >>= **fun**(*x*) { ... }. The operator name <=<= can be any binary operator name, the corresponding operator name >>= in the semantically equivalent expression is always derived by simply changing all '>' characters to '<' and changing all '<' characters to '>', i.e. by reversing the direction of those characters.

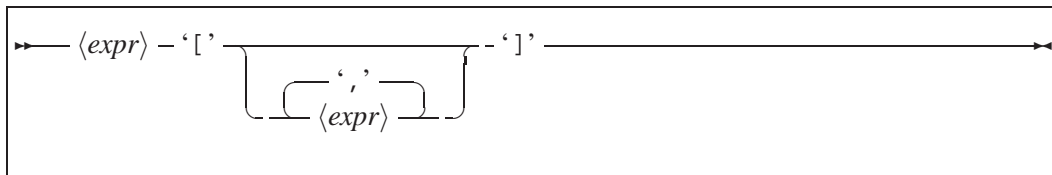
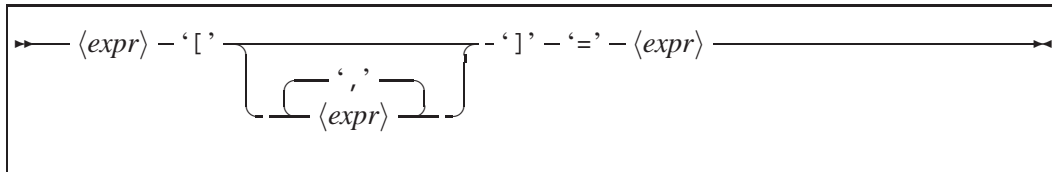
2.17 Array Expressions

Morpho supports both object-oriented and non-object-oriented arrays. Fetching a value from a non-object-oriented array or inserting a value into it is achieved by calling some function. In the case of object-oriented arrays the same things are achieved by sending messages to the array.

2.17.1 Non-Object-Oriented Arrays

Syntax diagrams 19 on the following page and 20 on the next page show the patterns of Morpho expressions used to fetch values from and store values into arrays. Note that these two diagrams, although they are syntactically correct, ignore the effects of the different precedences of the diverse syntactic constructs in Morpho. Diagram 56 on page 60 and related diagrams are more appropriate in that regard.

The following module defines simple-minded non-object-array of two position denoted by indexes 0 and 1.

Syntax Diagram 19: $\langle array_get_usage \rangle$ Syntax Diagram 20: $\langle array_set_usage \rangle$

```

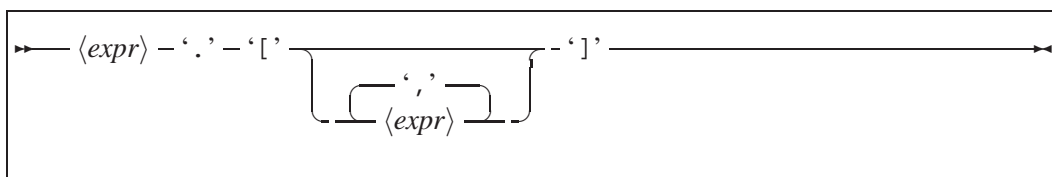
1 "simplearray.mmod" =
2 {{
3 makeSimpleArray =
4   fun()
5   {
6     []:[];
7   };
8
9 get[] =
10  fun(a,i)
11  {
12    i==0 && (return head(a));
13    return tail(a);
14  };
15
16 set[] =
17  fun(a,i,x)
18  {
19    if( i==0 )
20    {
21      setHead(a,x);
22      return x;
23    };
24    setTail(a,x);
25    x;
26  };
27 }}
28 ;

```

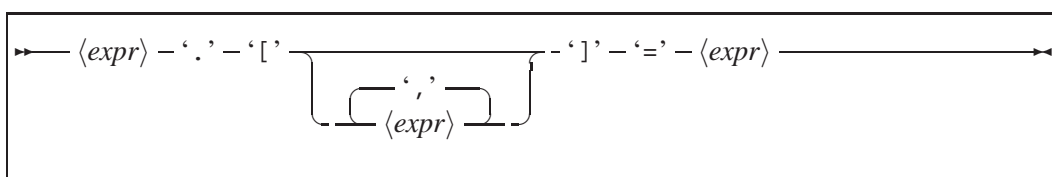
The two exported functions `get[]` and `set[]` are semantically just like any other Morpho functions. Syntactically, however, their names make them special in that they are called using expressions `a[i]` and `a[i]=e`, respectively, where `i` and `e` are any expressions. Similar holds for arrays of more than one dimension or fewer than one (i.e. zero) dimensions. A function with signature `fun(a, i1, ..., iN)` (i.e. a function taking `N+1` arguments) can be used as a `get[]` function for `N`-dimensional arrays, and a function with signature `fun(a, i1, ..., iN, x)` can be used as a `set[]` function. It is the programmers responsibility to make sure that these behave like array get and set functions.

2.17.2 Object-Oriented Arrays

Syntax diagrams 21 and 22 show the patterns of Morpho expressions used to fetch values from and store values into object-oriented arrays. Note that, as with the non-object-oriented arrays, these two diagrams, although they are syntactically correct, ignore the effects of the different precedences of the diverse syntactic constructs in Morpho. Again, diagram 56 on page 60 and related diagrams are more appropriate in that regard.



Syntax Diagram 21: `<obj_array_get_usage>`



Syntax Diagram 22: `<obj_array_set_usage>`

The following module defines simple-minded object-oriented array of two position denoted by indexes 0 and 1.

```

1 "simpleobjarray.mmod" =
2 {{
3 makeSimpleObjArray =
4   obj()
5   {
6     var pos0, pos1;

```

```

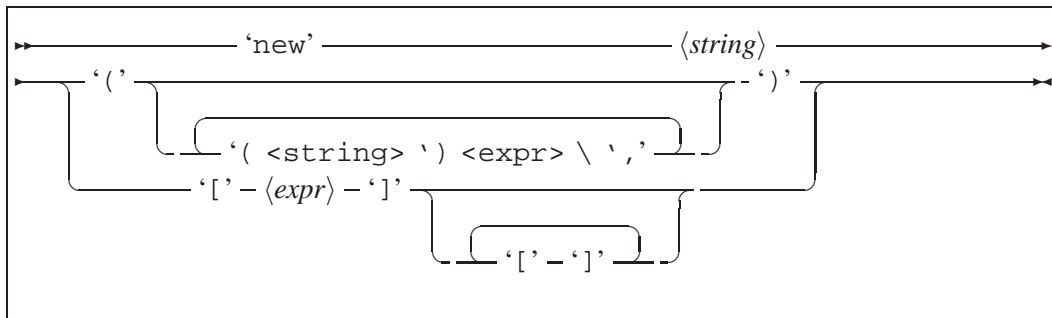
7   msg get[i]
8   {
9     i==0 && (return pos0);
10  return pos1;
11  };
12  msg set[i]=x
13  {
14    if( i==0 )
15    {
16      pos0 = x;
17      return x;
18    };
19    pos1 = x;
20    x;
21  };
22 };
23 }}
24 ;

```

The two messages `get[]` and `set[]` are semantically just like any other Morpho messages. Syntactically, however, their names make them special in that they are called using expressions `a.[i]` and `a.[i]=e`, respectively, where `i` and `e` are any expressions. Similar holds for arrays of more than one dimension or fewer than one (i.e. zero) dimensions. A message with signature `msg(i1, ..., iN)` (i.e. a message taking `N` arguments) can be used as a `get[]` message for `N`-dimensional arrays, and a message with signature `msg(i1, ..., iN, x)` can be used as a `set[]` message. It is the programmers responsibility to make sure that these behave like array `get` and `set` messages.

2.18 Java Construction Expressions

Morpho has a special expression to directly construct a Java object using a Java class constructor. Diagram 23 on the following page shows the pattern of the Java object construction expression. The effect of an expression `l$inline|new "A"(("B1")e1,...,("Bn")en)|` is to call a Java class constructor for class `A` with arguments `e1, ..., en`. The constructor called is found by searching for a constructor that takes `n` arguments of types `B1, ..., Bn`. If no such constructor exists or if the values returned by the expressions `e1, ..., en` are not of types `B1, ..., Bn` then a run-time exception will occur. If no error occurs the value of the expression will be a reference to the newly created object of type `A`.

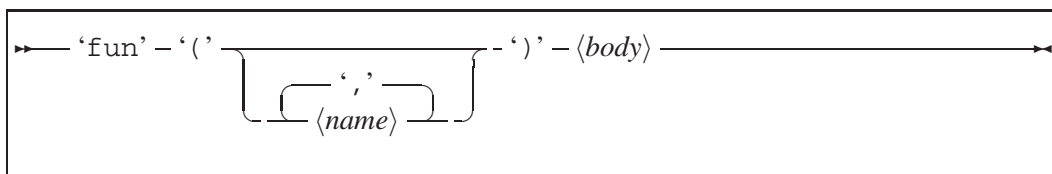
Syntax Diagram 23: $\langle java_construction_expr \rangle$

2.19 Delayed-Evaluation Expressions

Morpho has expressions that delay execution of contained expressions. The simplest such expression is the function expression.

2.19.1 Function Expression

Diagram 24 shows the pattern of the anonymous function expression. Such

Syntax Diagram 24: $\langle anonymous_fun_def \rangle$

function values can be assigned to variables, returned as values from functions, and in general sent anywhere, just like any other Morpho values. The following program code shows examples.

```

1 "funexample.mexe" = main in
2 {{
3 main =
4   fun()
5   {
6     var f,g,x;
7     f = fun(z){z+x;};
8     x = 10;
9     writeln(f(1));           ;;; Writes 11
10    g = f;
11    x = 100;
12    writeln(g(1));           ;;; Writes 101
13    x = 1000;

```

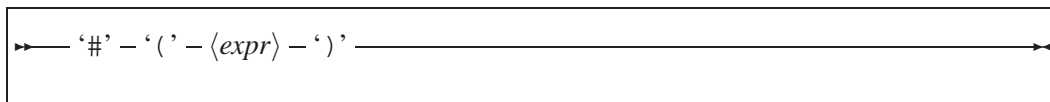
```

14     writeln(fun(z){z+x;}(1));   ;; Writes 1001
15   }i
16 }}
17 *
18 BASIS
19 ;

```

2.19.2 Memoized Delay

Diagram 25 shows the pattern of the delay expression. Evaluating a delay expres-

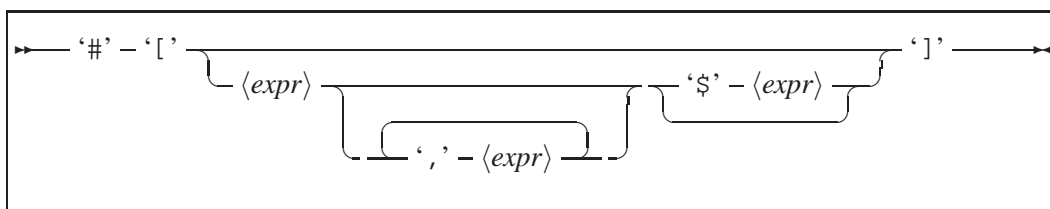


Syntax Diagram 25: $\langle delay_expr \rangle$

sion does not cause the enclosed expression to be evaluated but instead creates a *promise* that can later be evaluated using the `force` function in the BASIS module. The two expressions `e` and `force(#(e))` are semantically equivalent for any expression `e`. However, forcing a promise a second time (or more times) does not cause subsequent evaluations but rather causes the result of the first evaluation to be returned each time. If multiple Morpho tasks attempt to force the same promise only one task will be allowed to start evaluating the subexpression. The other tasks will be blocked until the first evaluation succeeds and will then receive the result from that first evaluation. Because a promise remembers the result of its first evaluation this is sometimes called *memoization*. We say that the result of the computation is *memoized*.

2.19.3 Stream Expression

Stream expressions are used to construct sequences where the values in the sequence are generated on demand. Diagram 26 shows the pattern of stream expressions. Stream expressions, like the delayed evaluation expressions above, are



Syntax Diagram 26: $\langle stream_expr \rangle$

really just syntactic sugar, i.e. they are more convenient ways of expressing things that can already be expressed in other ways in Morpho.

- A stream expression `#[]` is equivalent to the expressions `[]` and `null`.
- A stream expression `#[e]`, where `e` is a single expression, is equivalent to `[e$#([])]`. Please note two consequences of the embedded delay expression.
 - The computation of the tail is memoized (see above).
 - If multiple tasks attempt evaluation of the tail of a stream only one of the tasks will be allowed to perform the evaluation. The other tasks will be blocked until the result is ready.
- A stream expression `#[e1, ...]` is equivalent to `[e1$#(#[...])]`.
- A stream expression `#[e1$e2]` is equivalent to `[e1$#(e2)]`, which is equivalent to `e1:#(e2)`.

There are also two BASIS functions, `streamHead` and `streamTail` for deconstructing streams. `streamHead` returns the head of a stream while `streamTail` returns its tail.

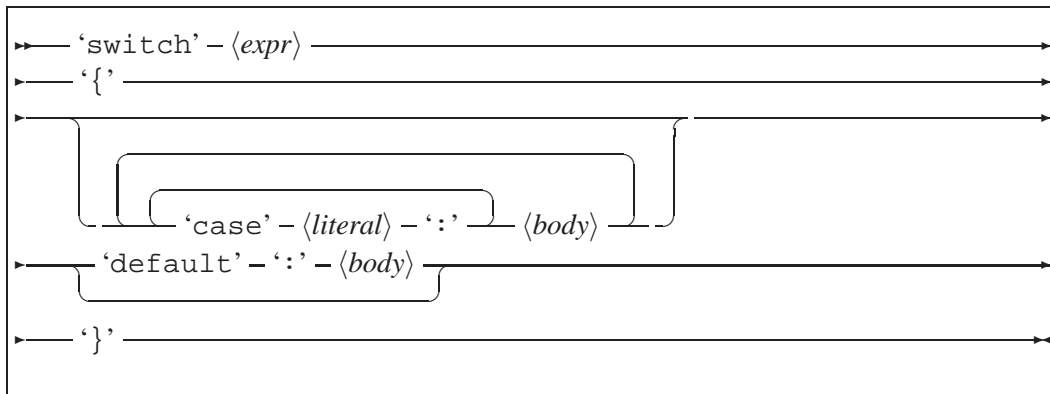
The following relations hold.

- `streamHead(#[e1$e2])` returns the same value as `e1`.
- `streamTail(#[e1$e2])` returns the same value as `e2`.

Note the similarity of these stream relations to the relations that hold for lists, i.e.

- `head([e1$e2])` returns the same value as `e1`.
- `tail([e1$e2])` returns the same value as `e2`.

The difference is in the way the tail is evaluated. In the case of lists, when the expression `[e1$e2]` is evaluated, the subexpression `e2` is immediately evaluated. In the case of streams, on the other hand, when the expression `#[e1$e2]` is evaluated, the subexpression `e2` is *not* immediately evaluated. The expression `e2` will be evaluated the first time the function `streamTail` is applied to the result of evaluating `#[e1$e2]`. Note also that for any value `x` the expressions `streamTail(x)` and `force(tail(x))` are equivalent, assuming that the functions applied are the ones in the BASIS module.

Syntax Diagram 27: $\langle \text{switch_expr1} \rangle$

2.20 The ‘switch’ Expression

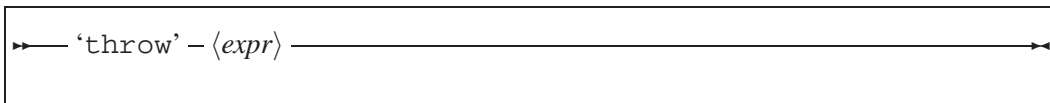
Diagram 27 (same as diagram 64 on page 63) shows the pattern of the switch expression. The effect of the switch expression is to evaluate $\langle \text{expr} \rangle$ and then search in some order through the cases and look for a literal that returns the same value as the expression. If such a literal is found then the corresponding body is evaluated and the resulting value becomes the value of the switch expression. If no such literal can be found then the default body is evaluated, if present, and the resulting value becomes the value of the switch expression. If no matching literal can be found and no default is present then the switch expression returns some unspecified value. Those familiar with the switch expression in C and C++ should note that there is no fall-through in the Morpho switch expression as in C and C++. Neither is there any relationship between a switch expression and a break expression.

2.21 Exception Handling Expressions

Morpho supports exceptions in a fashion similar to Java, C# and C++. Any value can be thrown as an exception, as in C++, but contrary to the way Java and C# support exceptions.

2.21.1 The ‘throw’ Expression

Diagram 28 on the following page shows the pattern of the throw expression. The effect of a throw expression such as `throw e` where e is any Morpho expression, is to evaluate e , and throw the resulting value as an exception. This means abandoning the current computation in the current fiber in the current thread and

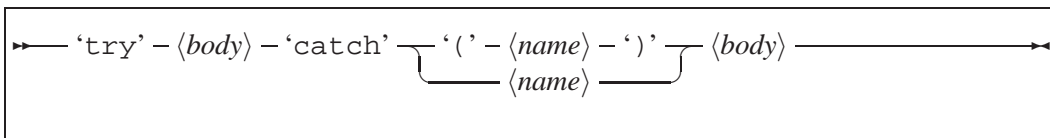


Syntax Diagram 28: $\langle throw\text{-}expr \rangle$

transferring control to the catch part of the most recently entered (and not exited) try part of a try-catch expression (see below).

2.21.2 The 'try-catch' Expression

Diagram 29 shows the pattern of the try-catch expression. The effect of a



Syntax Diagram 29: $\langle try\text{-}catch\text{-}expr \rangle$

try-catch expression such as `try{t1;...}catch(e){c1;...}` or the equivalent expression `try{t1;...}catch e {c1;...}` is to evaluate the try body `{t1;...}` and if an expression is thrown during that evaluation (and not caught by another try-catch) then the catch body `{c1;...}` is evaluated with the variable `e` being initialized with the value of the exception, i.e. the value resulting from the evaluation of the expression that is the argument of the throw expression (see above).

Chapter 3

Syntax

The Morpho syntax is reminiscent of C, C++, C# and Java.

3.1 Elements Of The Language

3.1.1 Keywords

Morpho has the following keywords:

`'break' 'case' 'catch' 'const' 'continue' 'default' 'else' 'elsif' 'false'`
`'fibervar' 'final' 'for' 'fun' 'if' 'in' 'machinevar' 'msg' 'new' 'null'`
`'obj' 'taskvar' 'rec' 'return' 'seq' 'super' 'switch' 'this' 'throw' 'true'`
`'try' 'val' 'var' 'while'`

3.1.2 More language elements

There are several kinds of literals and language elements in Morpho.

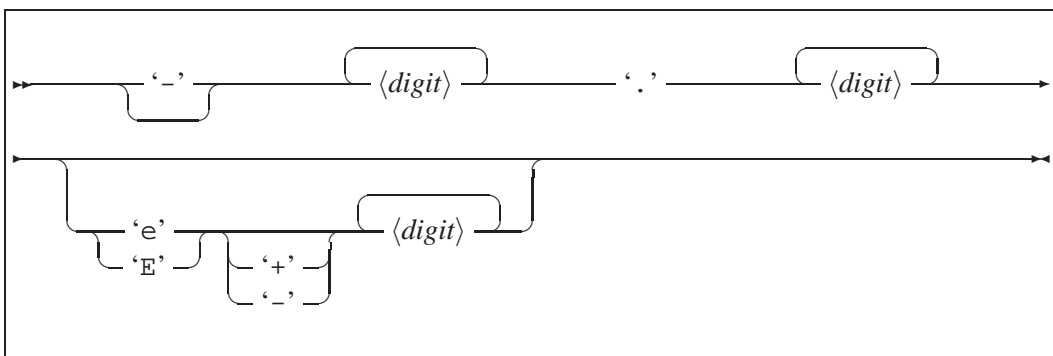
- Integer literals are described by syntax diagram 30 on the following page.
- Floating point (double) literals are described by syntax diagram 32 on the next page.
- Character literals are described by syntax diagram 33 on page 49.
- String literals are described by syntax diagram 34 on page 49.
- Literals in general are described by syntax diagram 36 on page 50.
- Names are described by syntax diagram 37 on page 50.
- Operation names are described by syntax diagram 39 on page 51.



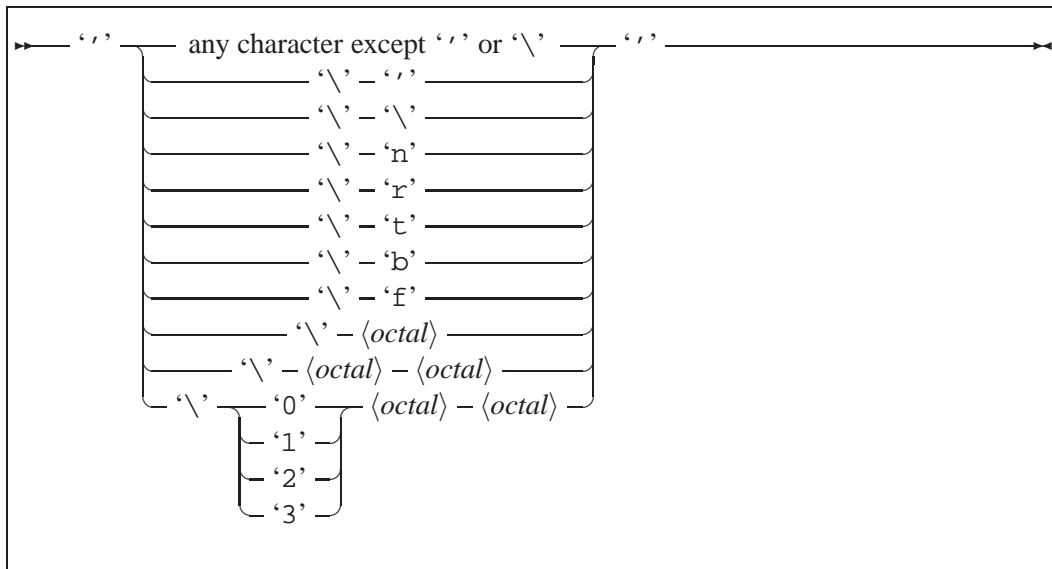
Syntax Diagram 30: $\langle integer \rangle$



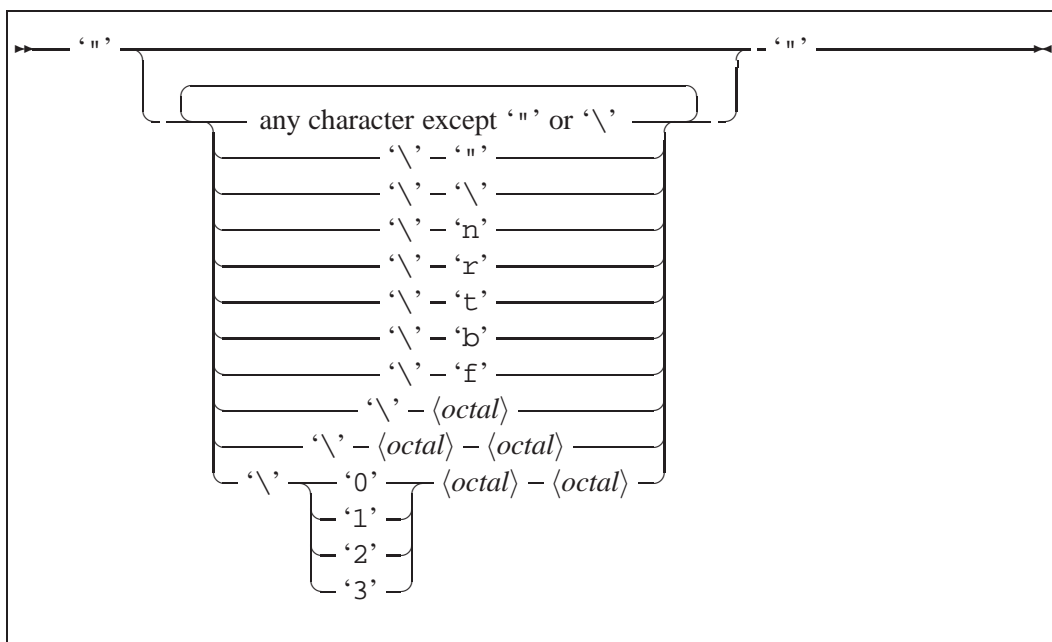
Syntax Diagram 31: $\langle digit \rangle$



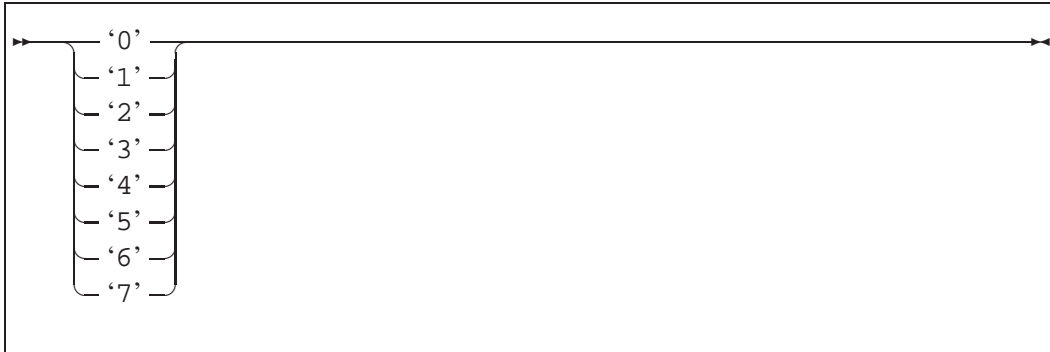
Syntax Diagram 32: $\langle double \rangle$



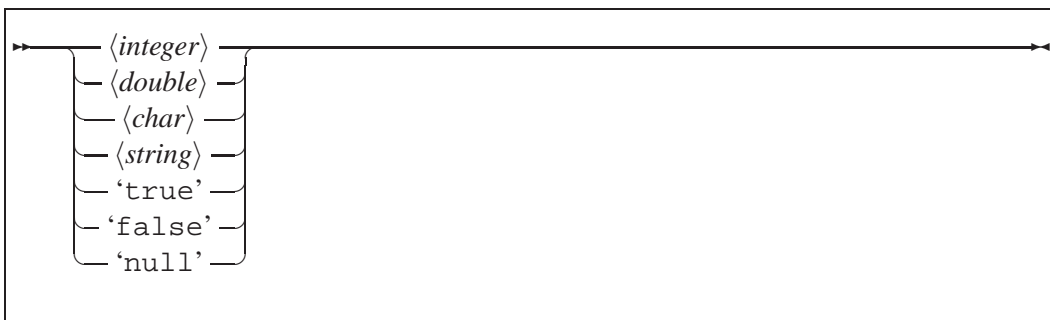
Syntax Diagram 33: $\langle char \rangle$



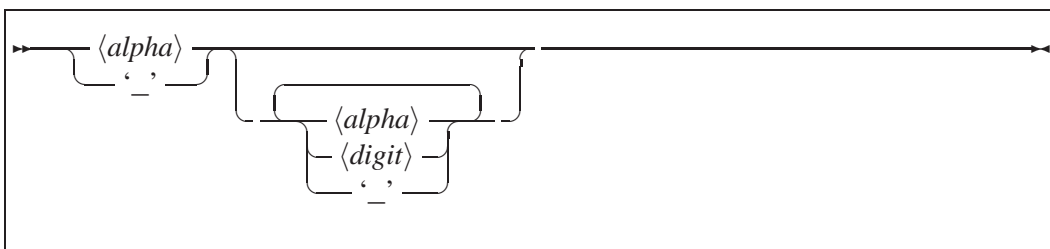
Syntax Diagram 34: $\langle string \rangle$



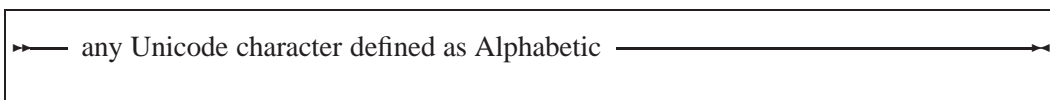
Syntax Diagram 35: `<octal>`



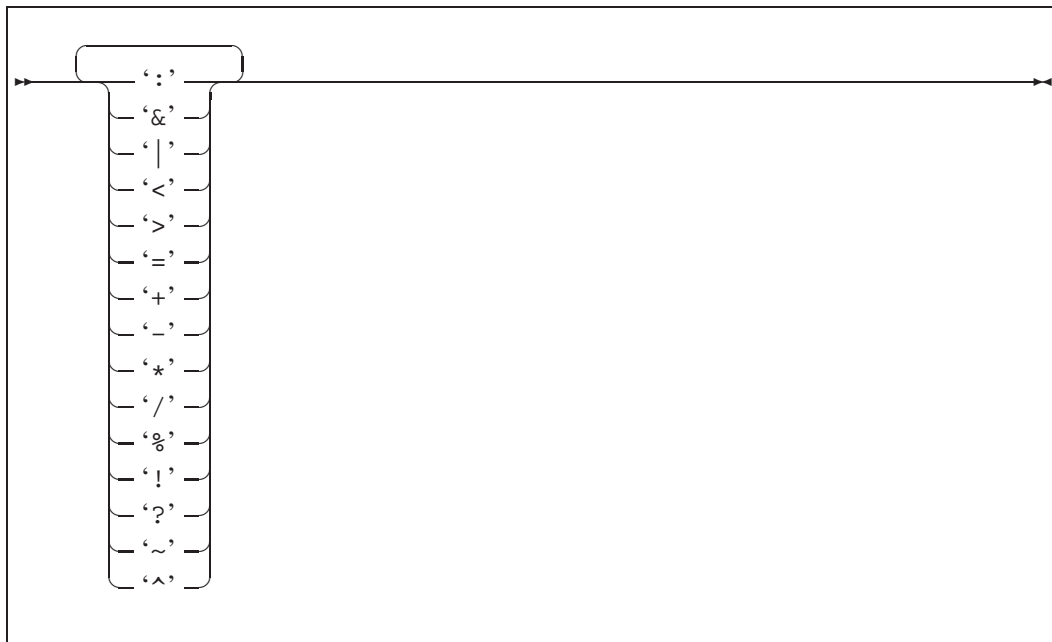
Syntax Diagram 36: `<literal>`



Syntax Diagram 37: `<name>`



Syntax Diagram 38: `<alpha>`

Syntax Diagram 39: $\langle opname \rangle$

3.1.3 Special Symbols

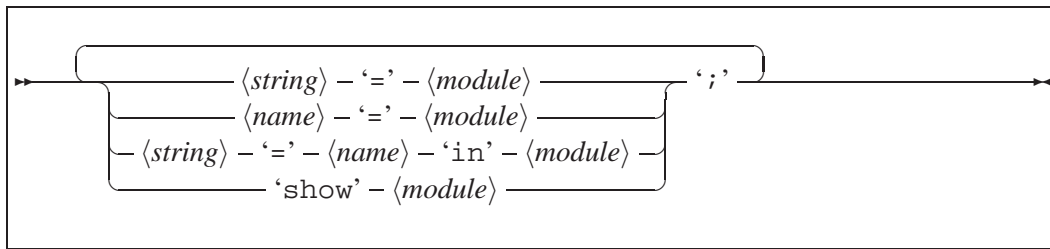
Morpho has the following special symbols: '(', ')', '{', '}', '[', ']', '\$', '#', ';', ',', '.', and '\'. In addition to each of these symbols having their special meaning, the special symbols act as delimiters between other elements of the language as does white space (space, newlines and tabbing characters).

3.1.4 Comments

Comments can be anywhere that white space is allowed, i.e. between any lexical elements (elements of the language). There are two types of comments, line comments and multiline comments. Line comments start with ';;;' and extend to the end of the line. Multiline comments start with '{;;;' and extend to a closing ';;;}'. Nested multiline comments are allowed, i.e. a multiline comment may, anywhere, contain a nested multiline comment, and the closing ';;;}' for the nested comment does not close the outer comment.

3.2 High-Level Syntax

3.2.1 Morpho Program

Syntax Diagram 40: $\langle program \rangle$

Syntax diagram 40 shows the syntax of a Morpho program, i.e. a compilation unit. A Morpho compilation unit is a sequence of compilation commands. A compilation command does one of the following:

- Compiles a module into a file.
- Compiles a module into a module variable.
- Compiles a program into a file.
- Shows the contents of a module.

For example, the following code creates the module file `reverse.mmod` which contains the single function `reverse`. The last line of this code is a `show` command that causes a description of the module to be written to the screen during compilation.

```

1 "reverse.mmod" =
2 {{
3 reverse =
4     fun(x)
5     {
6         var y=[];
7         while x
8         {
9             y = head(x) : y;
10            x = tail(x);
11        };
12        y;
13    };
14 }};
15
16 show "reverse.mmod" ;

```

Similarly, the beginning of the following code creates the module variable `rev` which contains the same module as above, which can then be used subsequently in

the same code file, but will be forgotten once the compilation of that file finishes. The module variable is then used, in this example, in the creation of an executable file, `rev.mexe`.

```

1 rev =
2 {{
3 reverse =
4     fun(x)
5     {
6         var y=[];
7         while x
8         {
9             y = head(x) : y;
10            x = tail(x);
11        };
12        y;
13    };
14 }};
15
16 "rev.mexe" = main in
17 {{
18 main =
19     fun()
20     {
21         writeln(reverse([1,2,3,4]));
22     };
23 }}
24 *
25 rev
26 *
27 BASIS
28 ;

```

The same executable could have been created as follows, assuming the existence of the module file `reverse.mmod`.

```

1 "rev.mexe" = main in
2 {{
3 main =
4     fun()
5     {
6         writeln(reverse([1,2,3,4]));
7     };
8 }}
9 *

```



```

10 "reverse.mmod"
11 *
12 BASIS
13 ;

```

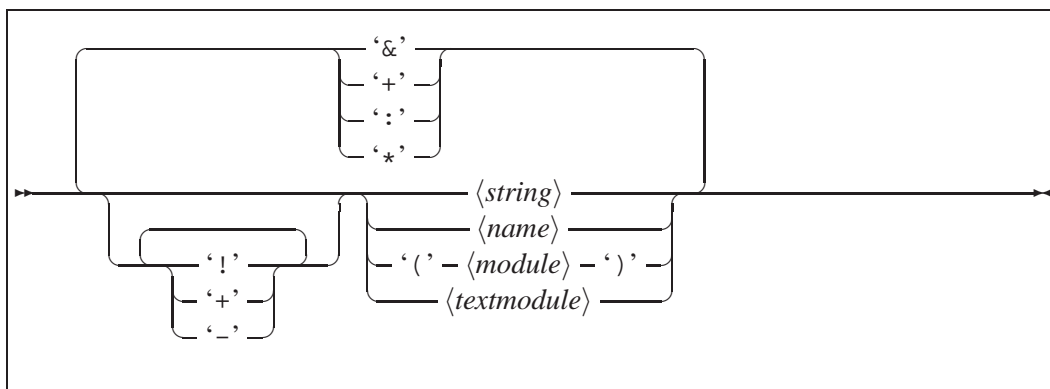
3.2.2 Modules

Syntax diagram 41 shows the syntax of a Morpho module. As the diagram indicates, modules can be composed using the binary operations '&', '+', ':', and '*', and they can be operated on by the unary operations '!', '+', and '-'. The unary operations have the highest precedence. Among the binary operations the '&' operation (link operation) has the lowest precedence. The '+' operation (join operation) has the next higher, the ':' operation (compose operation) the next, and finally the '*' (importation operation) has the highest precedence among the binary operations. Parentheses can be used to modify the application of the operations in the usual fashion.

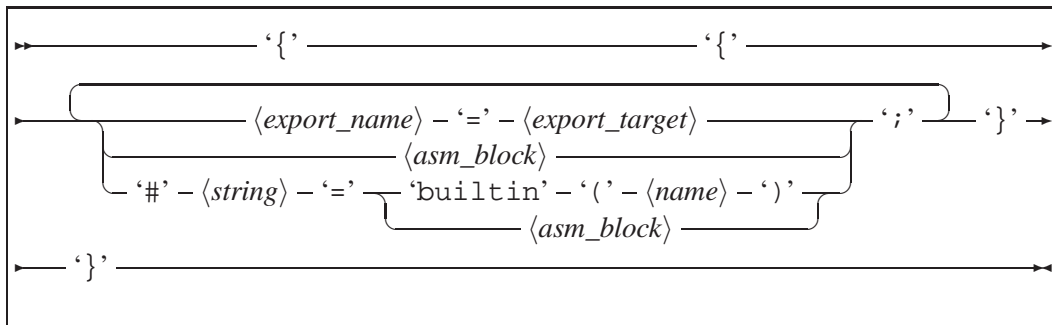
The semantics of the module operations are described elsewhere.

The simplest modules are:

- A string, which represents a preexisting modules loaded from a file.
- A name, which represents a preexisting module loaded from a module variable.
- A text module, which represents a module created from scratch with Morpho source code or with Morpho assembly language, the semantics of which is not described in this manual.



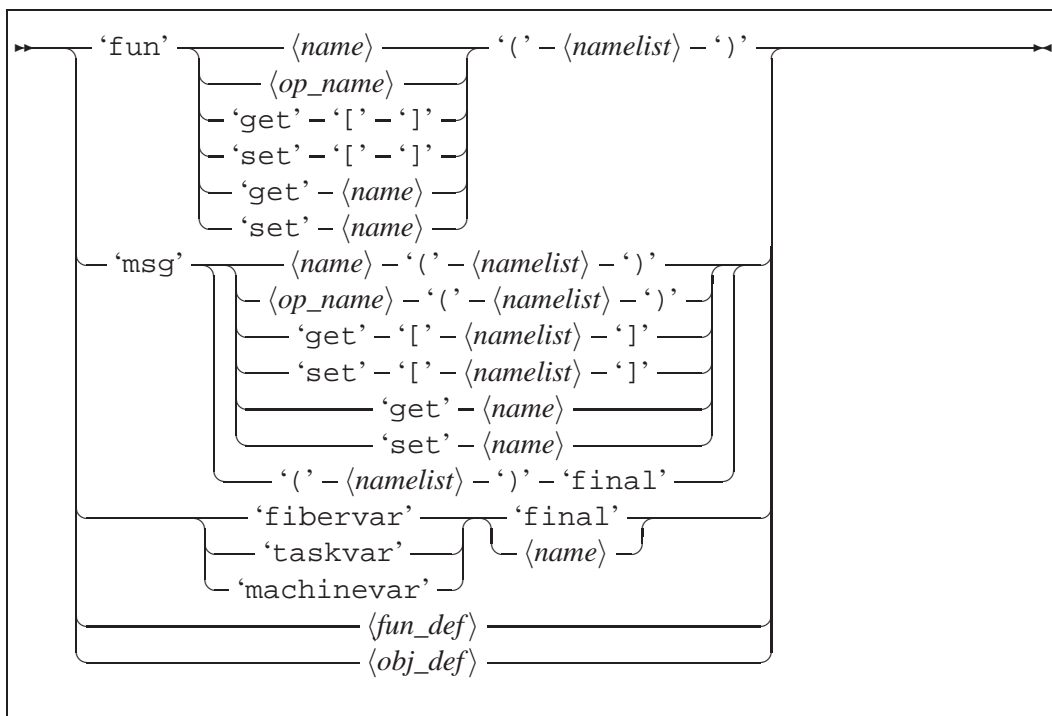
Syntax Diagram 41: $\langle module \rangle$



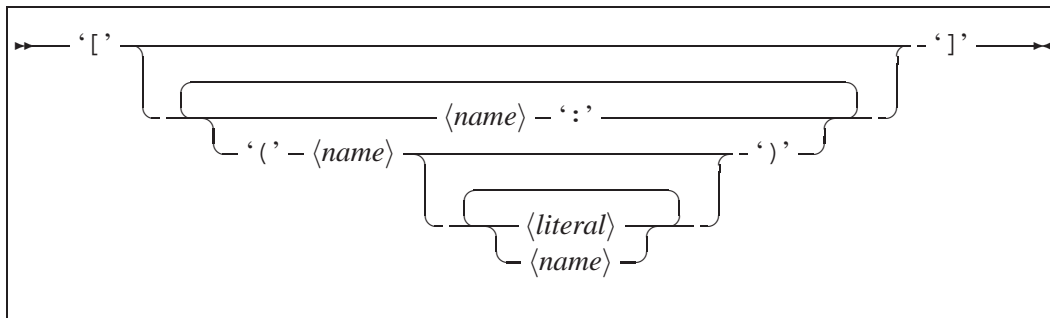
Syntax Diagram 42: `<textmodule>`



Syntax Diagram 43: `<export_name>`

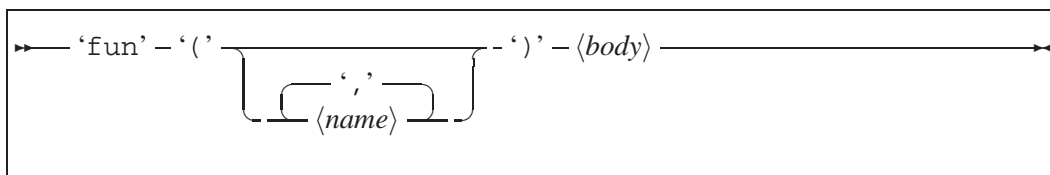


Syntax Diagram 44: `<export_target>`

Syntax Diagram 45: `<asm_block>`

3.2.3 Function Definitions

Syntax diagram 46 shows the syntax of a function definition. This syntax pattern describes both top-level functions that are exported from a module and nested functions inside other functions or object definitions. As with functions in most other programming languages Morpho functions are invoked using call expressions (described elsewhere) which cause the function to be executed.

Syntax Diagram 46: `<fun_def>`

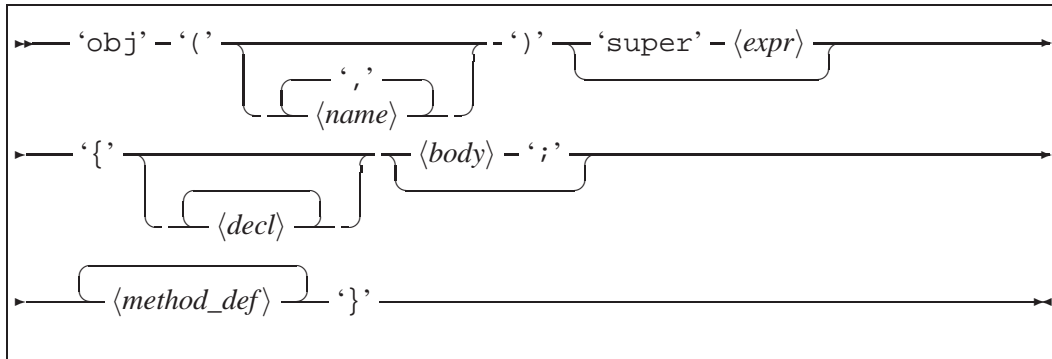
3.2.4 Object Definitions

Syntax diagram 47 on the following page shows the syntax of a Morpho object definition. This syntax pattern describes both top-level object definitions that are exported from a module and nested object definitions inside other functions or object definitions. A Morpho object definition is invoked as a function call, which causes a new instance of a corresponding object to be created and returned.

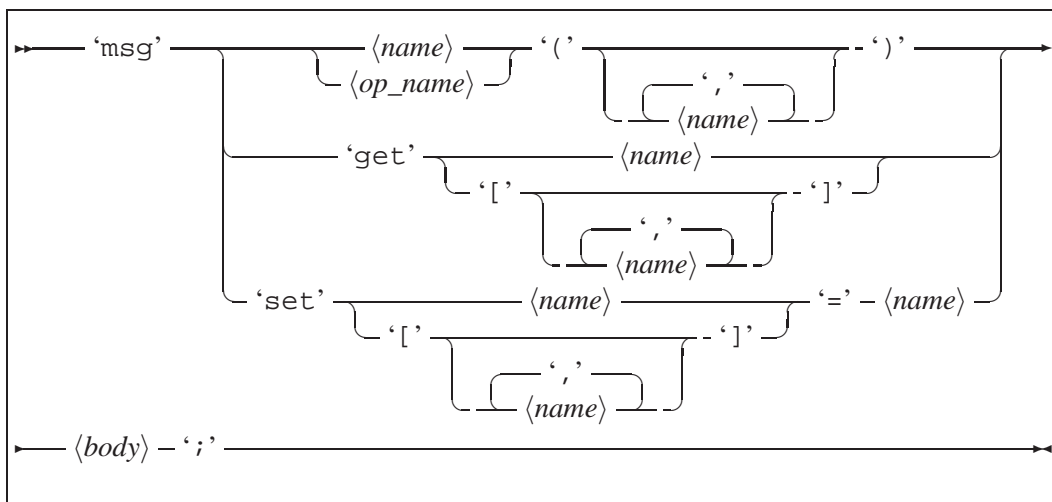
3.2.5 Body

Syntax diagram 49 on the next page shows the syntax of a Morpho code body. Such bodies are parts of various syntax patterns and stand for an executable sequence of expressions, optionally preceded by declarations.

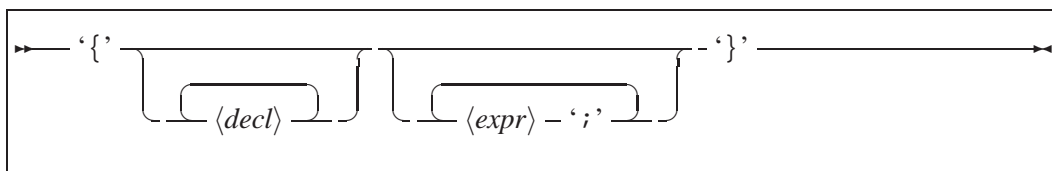
3.2.6 Declarations



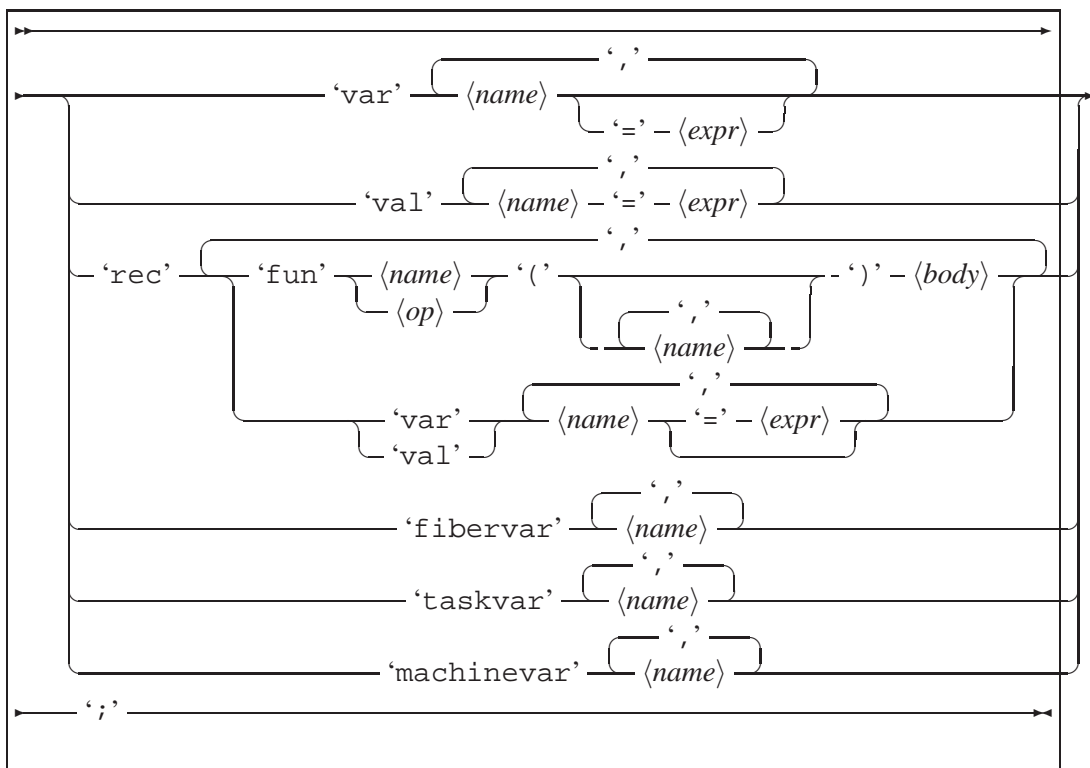
Syntax Diagram 47: $\langle obj_def \rangle$



Syntax Diagram 48: $\langle method_def \rangle$

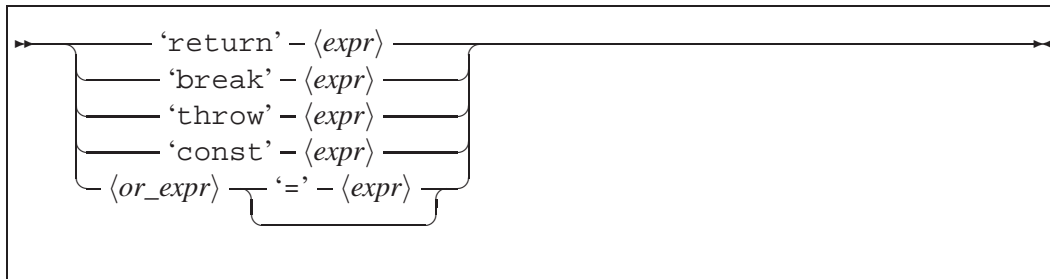


Syntax Diagram 49: $\langle body \rangle$



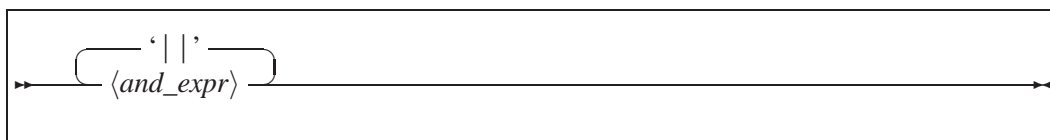
Syntax Diagram 50: $\langle decl \rangle$

3.2.7 Expressions

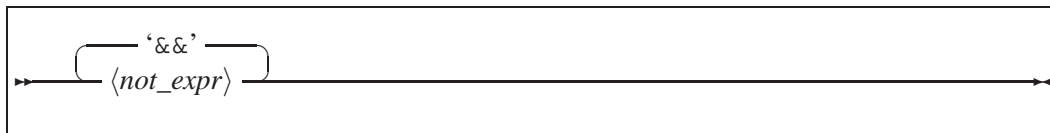


Syntax Diagram 51: $\langle expr \rangle$

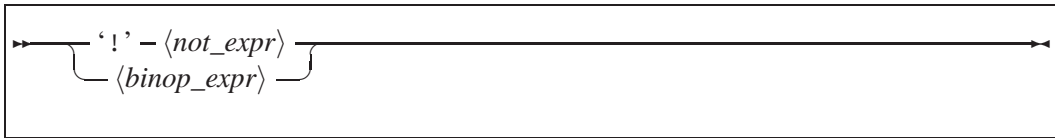
Note that the only semantically valid assignment targets are variables ($\langle name \rangle$), fields ($\langle expr \rangle.\langle name \rangle$ and $\langle expr \rangle.\#\langle name \rangle$ and $\langle expr \rangle.\#\langle string \rangle$ and $\langle expr \rangle.\#\#\langle name \rangle$ and $\langle expr \rangle.\#\#\langle string \rangle$), and array items ($\langle expr \rangle[\dots]$). The compiler will generate an error if the target of an assignment is not semantically valid.



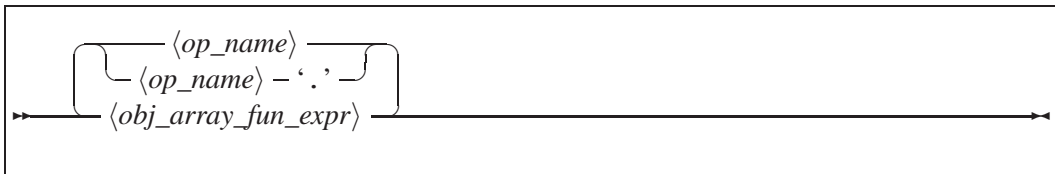
Syntax Diagram 52: $\langle or_expr \rangle$



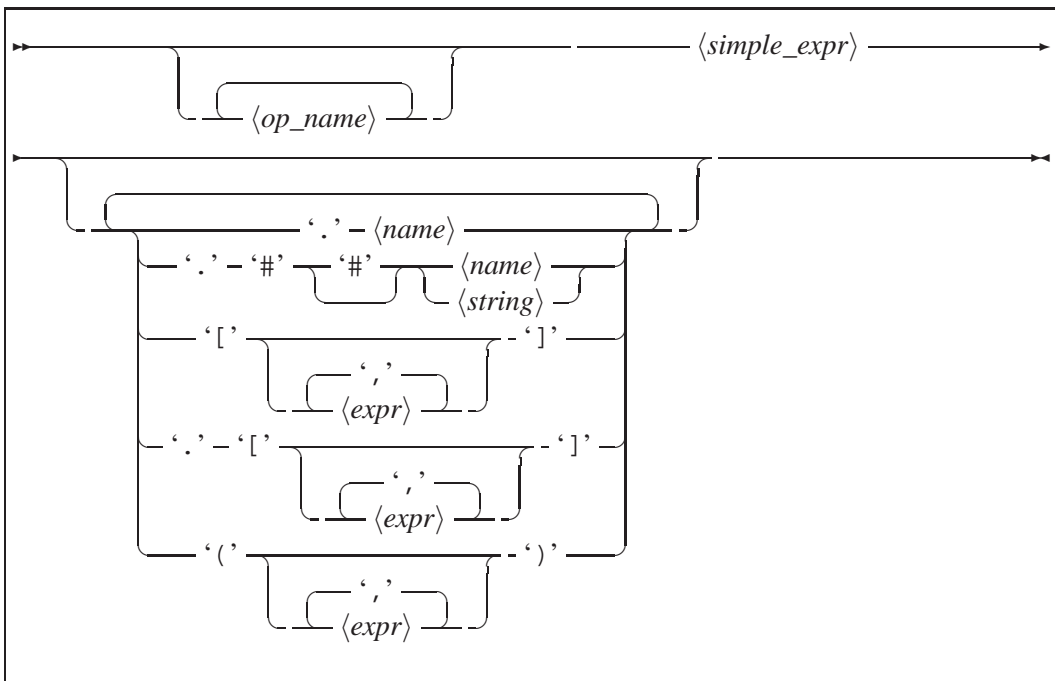
Syntax Diagram 53: $\langle and_expr \rangle$



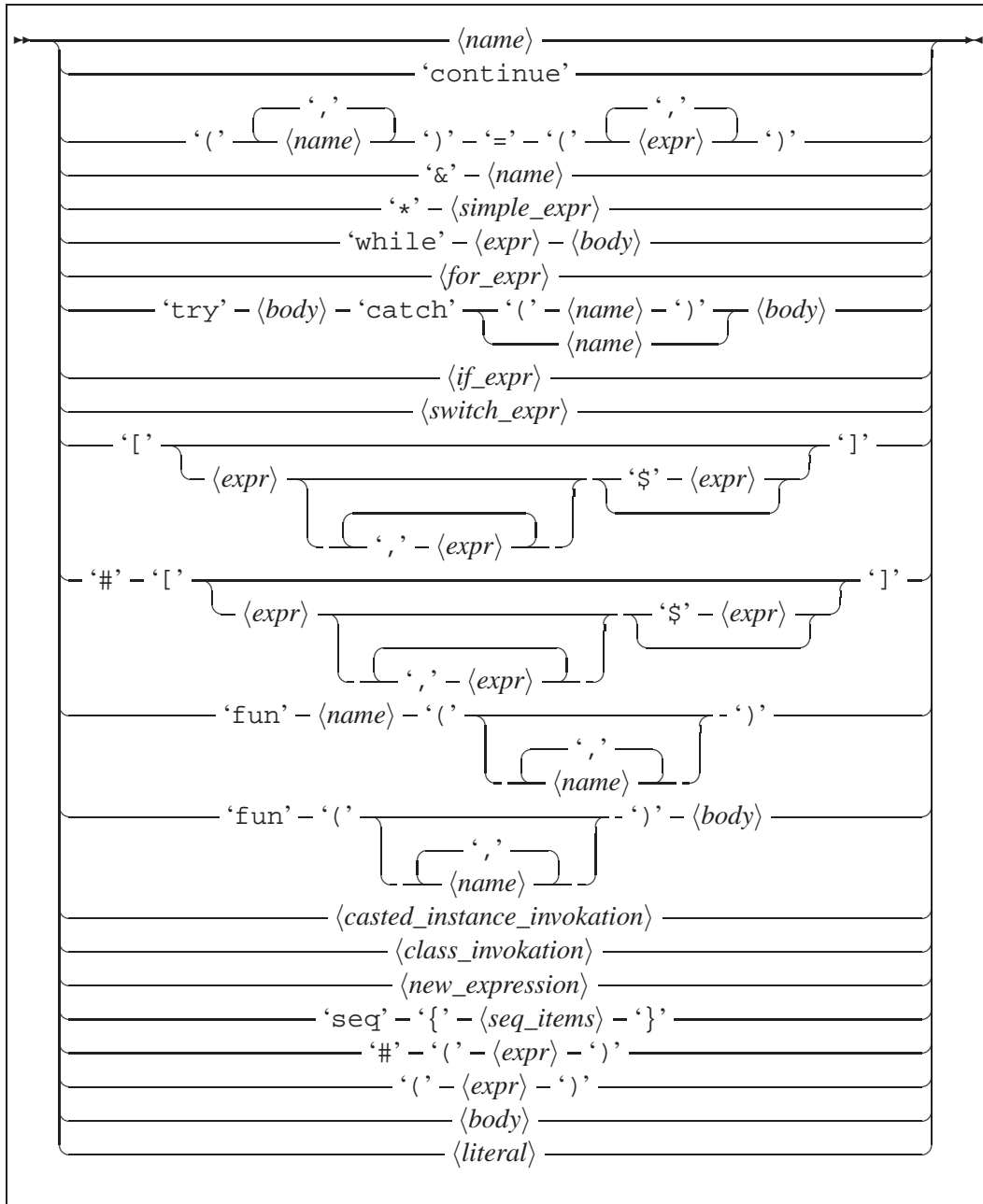
Syntax Diagram 54: $\langle not_expr \rangle$



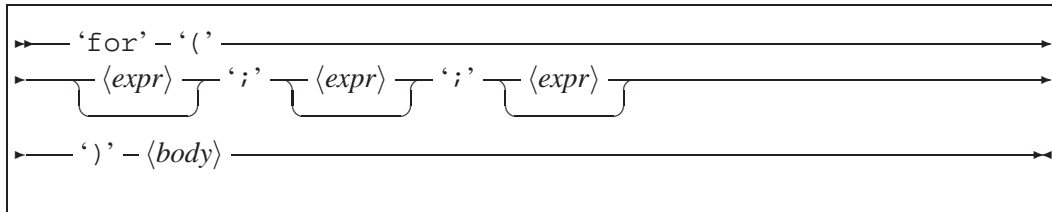
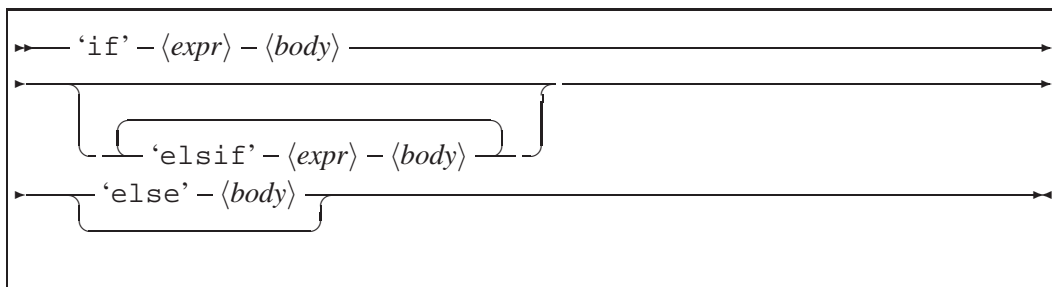
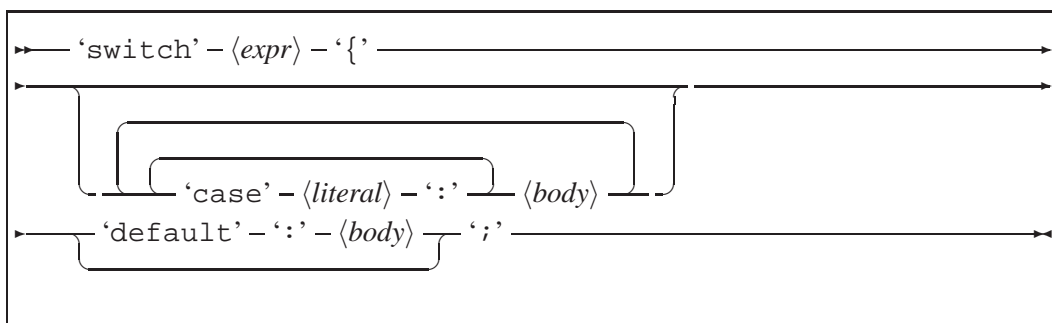
Syntax Diagram 55: $\langle binop_expr \rangle$



Syntax Diagram 56: $\langle obj_array_fun_expr \rangle$



Syntax Diagram 57: <simple_expr>

Syntax Diagram 62: $\langle for_expr \rangle$ Syntax Diagram 63: $\langle if_expr \rangle$ Syntax Diagram 64: $\langle switch_expr \rangle$

Chapter 4

Modules

Morpho has a unique way of handling modules. In Morpho we consider a module to be a first order substitution mapping names to values. Each module maps a finite set of names. A name can be mapped to one of the following:

- a function,
- an object constructor (actually an object constructor is a function),
- a message,
- a static variable, or
- another name.

4.1 Importation

Figure 4.1 on the following page shows a general example of module importation.

4.2 Join

Figure 4.2 on the next page shows a general example of module join.

4.3 Iteration

Figure 4.3 on page 66 shows a general example of module iteration.

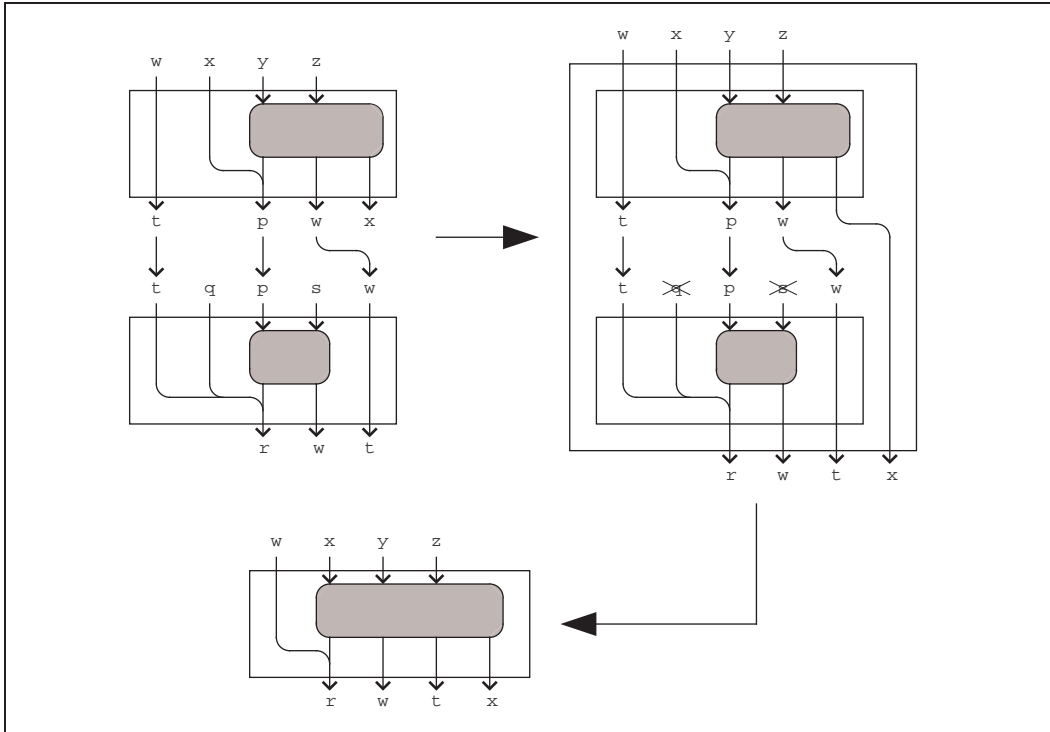


Figure 4.1: Module Importation

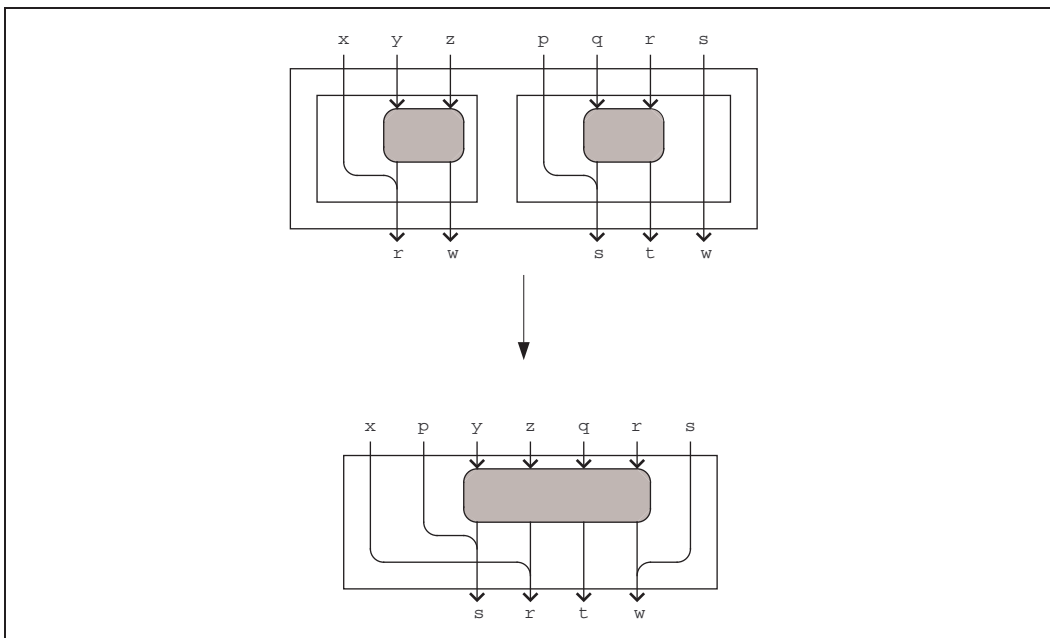
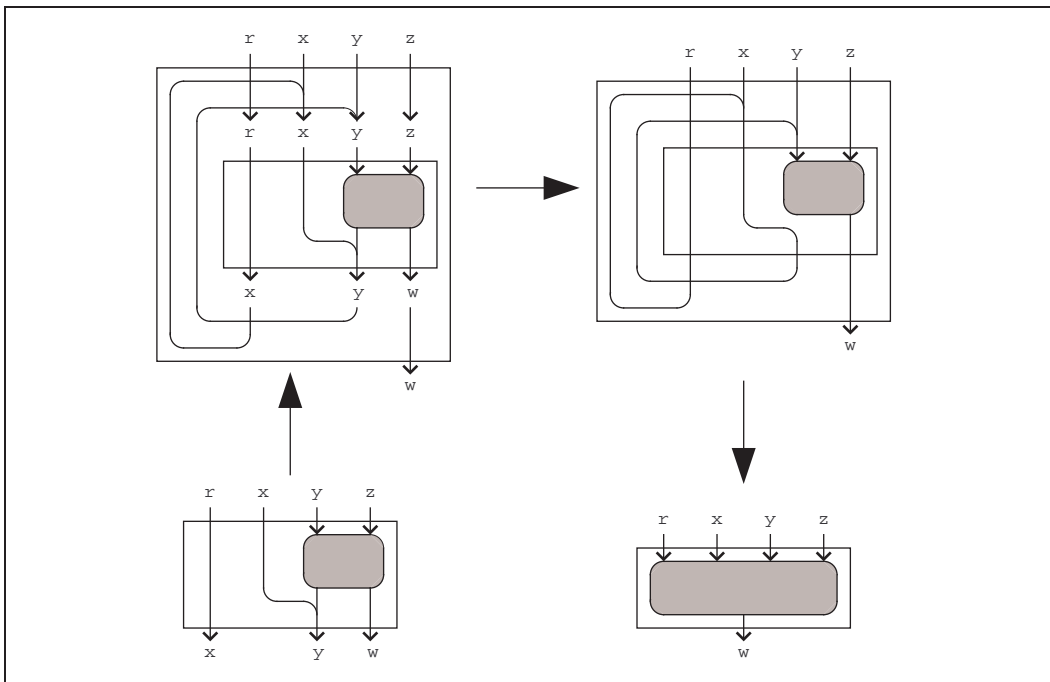


Figure 4.2: Module Join

**Figure 4.3:** Module Iteration

4.4 Composition

Figure 4.4 on the next page shows a general example of module composition.

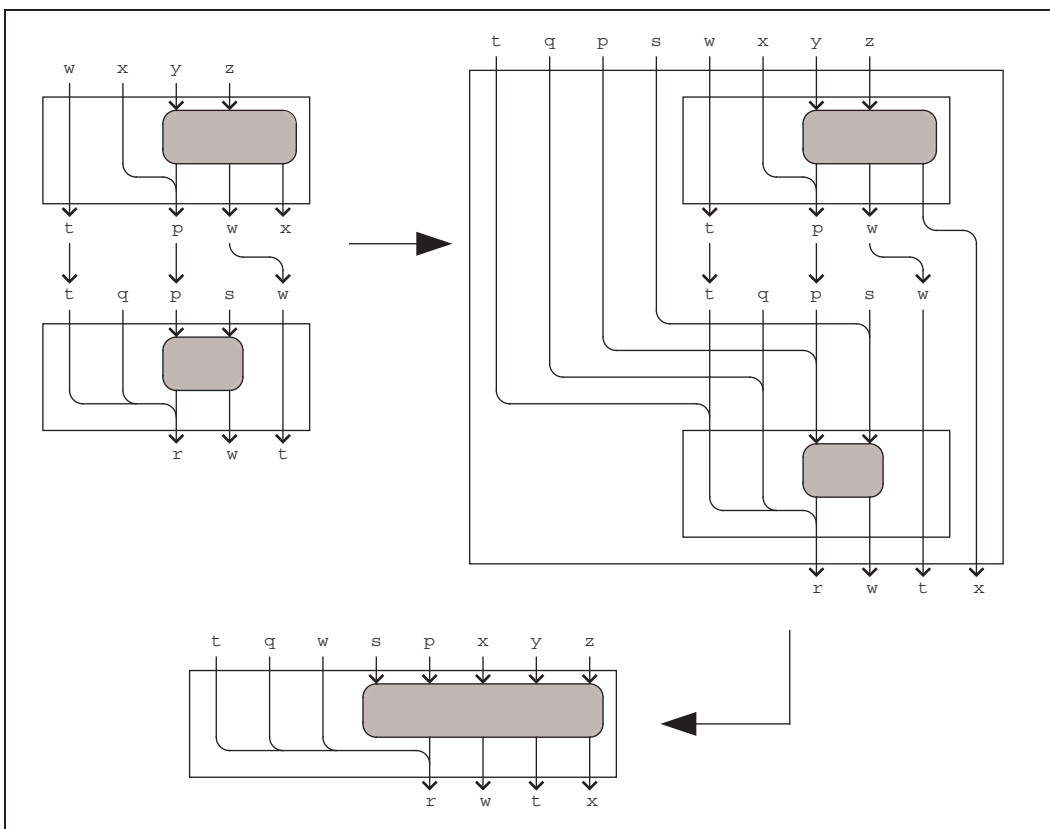


Figure 4.4: Module Composition

Part II
The BASIS Module

-

Use: $z = x - y;$

Pre: x and y should be numbers.

Post: z is the result of subtracting y from x . If both are integers, the result is an integer. If both are double, the result is double.

-

Use: $y = -x;$

Pre: x should be a number.

Post: y is the result of subtracting x from zero. If x is an integer, the result is an integer. If x is a double, the result is double.

!=

Use: $b = x != y;$

Pre: x and y can be any values.

Post: b is true if one is null but not the other or if they are objects that are not equal.

%

Use: $z = x \% y;$

Pre: x and y should both be integers and y should be positive.

Post: z is the remainder when x is divided by y .

*

Use: $z = x * y;$

Pre: x and y should be numbers.

Post: z is the result of multiplying y and x . If both are integers, the result is an integer. If both are double, the result is double.

/

Use: $z = x / y;$

Pre: x and y should be numbers, y should not be zero.

Post: z is the result of dividing x by y . If both are integers, the result is an integer.
If both are double, the result is double.

:

Use: $z = x : y;$

Pre: x and y can be any values.

Post: z is a new pair with x as head and y as tail.

+

Use: $z = x + y;$

Pre: x and y should be numbers.

Post: z is the result of adding y and x . If both are integers, the result is an integer.
If both are double, the result is double.

++

Use: $z = x ++ y;$

Pre: x should be a string and y can be any value.

Post: z is the result of appending y to x . If y is not a string it is converted to a string using the `toString()` Java method.

<-

Use: $c <- x;$

Pre: c is an open channel and x can be any value.

Post: The value x has been sent through the channel c .

<-

Use: $x = \text{<- } c;$

Pre: c is an open channel.

Post: The value x has been received through the channel c .

<

Use: $b = x < y;$

Pre: x and y should be Comparable and comparable to each other.

Post: b is true if x is less than y , false otherwise.

<=

Use: $b = x \leq y;$

Pre: x and y should be Comparable and comparable to each other.

Post: b is true if x is less than or equal to y , false otherwise.

==

Use: $b = x == y;$

Pre: x and y can be any values.

Post: b is true if both are null or if they refer to equal objects, false otherwise.

>

Use: $b = x > y;$

Pre: x and y should be Comparable and comparable to each other.

Post: b is true if x is greater than y , false otherwise.

>=

Use: $b = x \geq y;$

Pre: x and y should be Comparable and comparable to each other.

Post: b is true if x is greater than or equal to y , false otherwise.

>>=

Use: $y = x \gg= f;$

Pre: x should be a stream of values, f should be a function of one argument that returns a stream.

Post: y is the stream of values that is composed by concatenating the streams that result from feeding the values in the stream x to the function f . See also the function `streamConcatMap`.

abs

Use: $y = \text{abs}(x);$

Pre: x should be a Double.

Post: y is the absolute value of x .

acos

Use: $y = \text{acos}(x);$

Pre: x should be a Double between -1.0 and 1.0 , inclusive.

Post: y is the arc cosine of x , an angle between 0.0 and π .

Storing in Arrays

Use: $a[i] = x;$

Pre: a is either a Java Object array (`Object[]`) or a hashmap created by calling `makeHashMap`. If a is an Object array then i must be an integer value that is a valid index in that array. If a is a hashmap then i can be any value that fulfills the contracts of the Java `hashCode` and `equals` methods.

Post: The value of x has been stored in a under index i .

Fetching from Arrays

Use: $x = a[i];$

Pre: a is either an array (`T[]` for some type T) or a hashmap created by calling `makeHashMap`. If a is an Object array then i must be an integral value that is a valid index in that array. If a is a hashmap then i can be any value that fulfills the contracts of the Java `hashCode()` and `equals()` methods.

Post: The variable x contains the value stored in a under index i .

arrayGet

Use: `x = arrayGet(a, i);`

Pre: `a` is an array (`T[]` for some type `T`), `i` is an integer (byte, short, int, long or `BigInteger`).

Post: The variable `x` contains the value in position `i` of the array `a`.

arrayLength

Use: `n = arrayLength(a);`

Pre: `a` is an Object array (`Object[]`).

Post: The variable `n` contains the length of the array `a`.

arraySet

Use: `arraySet(a, i, x);`

Pre: `a` is an array (`T[]` for some type `T`), `i` is an integer (byte, short, int, long or `BigInteger`), `x` contains a value of type `T`.

Post: The the value in position `i` of the array `a` has been set to `x`.

asin

Use: `y = asin(x);`

Pre: `x` should be a `Double` between -1.0 and 1.0 , inclusive.

Post: `y` is the arc sine of `x`, an angle between $-pi/2$ and $pi/2$.

atan

Use: `y = atan(x);`

Pre: `x` should be a `Double`.

Post: `y` is the arc tangent of `x`, an angle between $-pi/2$ and $pi/2$.

atan

Use: `r = atan(y,x);`

Pre: `x` and `y` should be Double values, not both zero.

Post: `r` is the angle of the vector (x, y) , an angle between $-pi$ and pi .

atan2

Use: `r = atan2(y,x);`

Pre: `x` and `y` should be Double values, not both zero.

Post: `r` is the angle of the vector (x, y) , an angle between $-pi$ and pi .

Note: This is the same function as the binary `atan` function.

bigInteger

Use: `y = bigInteger(x);`

Pre: `x` must be BigInteger, Long, Integer, Short, Character or Byte.

Post: `y` now contains the same value, but as a BigInteger object.

byte

Use: `y = byte(x);`

Pre: `x` must be BigInteger, Long, Integer, Short, Character or Byte.

Post: `y` now contains the same value (if possible), but as a Byte object.

canReadChannel

Use: `b = canReadChannel(c);`

Pre: `x` must be a channel (an `is.hi.cs.morpho.Channel` object).

Post: `b` now contains true iff the channel can be read from without blocking.

canWriteChannel

Use: `b = canWriteChannel(c);`

Pre: `x` must be a channel (an `is.hi.cs.morpho.Channel` object).

Post: `b` now contains `true` iff the channel can be written to without blocking.

cbrt

Use: `y = cbrt(x);`

Pre: `x` should be a `Double`.

Post: `y` is the cube root of `x`.

channelEOF

Use: `eof = channelEOF();`

Post: `eof` contains a special `channelEOF` value that represents end-of-file on a channel.

char

Use: `y = char(x);`

Pre: `x` must be `BigInteger`, `Long`, `Integer`, `Short`, `Character` or `Byte`.

Post: `y` now contains the same ordinal value (if possible), but as a `Character` object.

classOf

Use: `c = classOf(x);`

Pre: `x` is any non-null value.

Post: The variable `c` contains a class object that is the class of `x`.

closeChannel

Use: `closeChannel(c);`

Pre: `c` must be a channel.

Post: `c` is now closed. All current and subsequent writes to the channel will immediately succeed without effect and all current and subsequent reads will immediately return the `channelEOF` value. See also the BASIS function `channelEOF`.

cos

Use: `x = cos(r);`

Pre: `r` should be a `Double`.

Post: `x` is the cosine of `r`.

dec

Use: `y = dec(x);`

Pre: `x` is an integer value.

Post: The variable `y` contains `x-1`.

double

Use: `y = double(x);`

Pre: `x` must be a `Float`, `Double`, `BigInteger`, `Long`, `Integer`, `Short`, `Character` or a `Byte`.

Post: `y` now contains the same value (as far as possible), but as a `Double` object.

exit

Use: `exit(n);`

Pre: `n` is an integer value.

Post: The program has exited with exit code `n`.

exp

Use: `y = exp(x);`

Pre: `x` should be a `Double`.

Post: `y` is e raised to the power `x`, e^x .

expm1

Use: `y = expm1(x);`

Pre: `x` should be a `Double`.

Post: `y` is e raised to the power `x`, minus 1, $e^x - 1$.

findField

Use: `field = findField(class, fieldName);`

Pre: `class` is a class, as returned by the `classOf` function or the `findClass` function, `fieldName` is a string that should be the name of a static class variable.

Post: `field` is a field designator, appropriate for use as argument in the `getField` function.

findMethod

Use: `method = findMethod(class, methodName, args);`

Pre: `class` is a class, as returned by the `classOf` function or the `findClass` function, `methodName` is a string that should be the name of a method in the class, `args` is a list of classes, as `class`.

Post: `method` is a method designator, appropriate for use as argument in the `invokeMethod` function.

force

Use: `x = force(y);`

Pre: `y` is a promise.

Post: `x` is the value of the promise. If the promise has not been forced before then the underlying expression has now just been evaluated once to get the value. If the promise was evaluated earlier then the value returned by that evaluation is returned again. Note that if multiple fibers or tasks force the same promise, only one of them will evaluate the underlying expression.

Example:

```
1   x = force(#(i+1));  
2   ;;; equivalent to: x = i+1;
```

format

Use: `s = format(f,v);`

Pre: `f` is a format string (see `java.util.Formatter`) and `v` is a value that the format string can format.

Post: `s` is a string that is the result of using the format string to format the value.

format

Use: `s = format(f,v1,v2);`

Pre: `f` is a format string (see `java.util.Formatter`), and `v1` and `v2` are values that the format string can format.

Post: `s` is a string that is the result of using the format string to format the values.

format

Use: `s = format(f,v1,v2,v3);`

Pre: `f` is a format string (see `java.util.Formatter`), and `v1`, `v2` and `v3` are values that the format string can format.

Post: `s` is a string that is the result of using the format string to format the values.

formatArray

Use: `s = format(f, arr);`

Pre: `f` is a format string (see `java.util.Formatter`), and `arr` is an `Object` array containing values that the format string can format.

Post: `s` is a string that is the result of using the format string to format the values.

from

Use: `s = from(i);`

Pre: `i` is an integer values.

Post: `s` is a stream of the integer values from `i`. More precisely, `s` is the infinite ascending stream of the integers `i, i+1, ...`

fromUpTo

Use: `s = fromUpTo(i, j);`

Pre: `i` and `j` are integer values.

Post: `s` is a stream of the integer values from `i` to `j`, inclusive. More precisely, `s` is the ascending stream of integers `k` fulfilling $i \leq k \leq j$.

Example:

```
1   ;;; Write 1..10
2   s = fromUpTo(1,10);
3   while s!=#[ ]
4   {
5       writeln(streamHead(s);
6       s = streamTail(s);
7   };
```

getArgs

Use: `args = getArgs();`

Post: `args` is a `String` array containing the command-line arguments of the currently running program.

getCurrentFiber

Use: `f = getCurrentFiber();`

Post: `f` is the current fiber state, i.e. a reference to the object representing the state of the current fiber. This object is automatically updated as the fiber progresses with its thread of computation. See also the BASIS functions `suspend`, `transfer`, `startFiber`, `makeFiber`, `makeFiberState`, and `suspend`.

head

Use: `y = head(x);`

Pre: `x` must be a pair.

Post: `y` contains the head of `y`.

Example: The code

```
1 {
2   val x=[1,2];
3   writeln(head(x));
4 }
```

will write the number 1.

hypot

Use: `z = hypot(x,y);`

Pre: `x` and `y` should be Double values.

Post: `z` is the length of the vector (x,y) .

inc

Use: `y = inc(x);`

Pre: `x` must be an integer value, i.e. a Byte, Short, Integer, Long or BigInteger.

Post: `y` contains the result from incrementing `x`, a value of the same type as `x`.

Example: The code

```
1 {  
2   writeln(inc(0));  
3 }
```

will write the number 1.

int

Use: `y = int(x);`

Pre: `x` must be `BigInteger`, `Long`, `Integer`, `Short`, `Character` or `Byte`.

Post: `y` now contains the same value (if possible), but as an `Integer` object.

isArray

Use: `b = isArray(a);`

Pre: `a` is any value.

Post: `b` now contains true iff `a` is an array.

isBigInteger

Use: `b = isBigInteger(i);`

Pre: `i` is any value.

Post: `b` now contains true iff `i` is a `BigInteger`.

isBoolean

Use: `b = isBoolean(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a `Boolean`.

isByte

Use: `b = isByte(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a `Byte`.

isChannelClosed

Use: `b = isChannelClosed(c);`

Pre: `c` is a channel.

Post: `b` now contains true iff `c` is closed.

isChar

Use: `b = isChar(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a Character.

isDouble

Use: `b = isDouble(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a Double.

isHashMap

Use: `b = isHashMap(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a Map object.

isInstanceOf

Use: `b = isInstanceOf(c, x);`

Pre: `x` is any value, `c` is a string that is a fully qualified class name.

Post: `b` now contains true iff `x` is an instance of the class denoted by `c`.

isInteger

Use: `b = isInteger(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is an Integer object.

isLong

Use: `b = isLong(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a Long object.

isPair

Use: `b = isPair(x);`

Pre: `x` can be any value.

Post: `b` contains true if and only if `x` is a pair (see also the binary operator ‘:’).

isShort

Use: `b = isShort(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a Short object.

isString

Use: `b = isString(x);`

Pre: `x` is any value.

Post: `b` now contains true iff `x` is a String object.

listToStream

Use: `y = listToStream(x);`

Pre: `x` must be a list, i.e. either `[]` (null) or a pair containing a tail that is a list.

Post: `y` now contains a stream that contains the same values as `x` in the same order.

log

Use: `y = log(x);`

Pre: `x` should be a positive Double.

Post: `y` is the natural logarithm of `x`.

log10

Use: $y = \log(x);$

Pre: x should be a positive Double.

Post: y is the base 10 logarithm of x .

log1p

Use: $y = \log1p(x);$

Pre: x should be a Double greater than -1.

Post: y is the natural logarithm of $x+1$.

long

Use: $y = \text{long}(x);$

Pre: x must be BigInteger, Long, Integer, Short, Character or Byte.

Post: y now contains the same value (if possible), but as a Long object.

makeArray

Use: $a = \text{makeArray}(n);$

Pre: n must be a non-negative BigInteger, Long, Integer, Short, Character or Byte.

Post: a now contains a new Object array of size n .

makeChannel

Use: $c = \text{makeChannel}();$

Post: c now contains a new channel (an `is.hi.cs.morpho.Channel` object).

makeChannelSelector

Use: `c = makeChannelSelector();`

Post: `c` now contains a new channel selector object, which is a Morpho object that facilitates multiplexing of channels. A channel selector has operations for adding subscriber channels and for starting multiplexing. To use a channel selector to monitor multiple channels for reading from them, you do the following:

1. Create the channel selector.
2. Add a read subscription to the channel selector for each of the channels you wish to monitor.
3. Start the channel selector, which gives you a channel to read from.
4. Read from the channel, which gives you a sequence of channels that are readable.
- 5.

Similarly, to use a channel selector to monitor multiple channels for writing to them, you do the following:

1. Create the channel selector.
2. Add a write subscription to the channel selector for each of the channels you wish to monitor.
3. Start the channel selector, which gives you a channel to read from.
4. Read from the channel, which gives you a sequence of channels that are writable.
- 5.

The channel selector has the following messages:

addReadSubscription

Usage: `sel.addReadSubscription(c);`

Pre: `sel` is a channel selector that has not been started and `c` is a channel.

Post: The channel selector now has a read subscription to the channel.

addWriteSubscription

Usage: `sel.addWriteSubscription(c);`

Pre: `sel` is a channel selector that has not been started and `c` is a channel.

Post: The channel selector now has a write subscription to the channel.

start

Usage: `c = sel.start();`

Pre: `sel` is a channel selector that has not been started.

Post: `c` refers to a newly created channel that will receive a sequence of channels. Each channel sent to `c` is either a channel that the channel selector has a read subscription to and is readable or a channel that the selector has a write subscription to and is writable.

makeFiber

Use: `f = makeFiber(c);`

Pre: `c` must be a function (a closure) that takes no argument.

Post: `f` now contains a new fiber state object that is associated with a fiber whose execution consists of calling the function `c` and then terminating. The fiber is not running but can be started by using it as the second argument in a call to the BASIS function `transfer`, or by calling the BASIS function `makeReady` with `f` as argument.

makeFiber

Use: `f = makeFiber(c, x);`

Pre: `c` must be a function (a closure) that takes one argument. `x` must be a valid argument to that function.

Post: `f` now contains a new fiber state object that is associated with a fiber whose execution consists of calling the function `c` with argument `x` and then terminating. The fiber is not running but can be started by using it as the second argument in a call to the BASIS function `transfer`, or by calling the BASIS function `makeReady` with `f` as argument.

makeFiberState

Use: `f = makeFiberState();`

Post: `f` now contains a new fiber state object that is not yet associated with any fiber. The fiber state can be associated with a fiber by using it as the first argument in a call to the BASIS function `transfer`.

makeHashMap

Use: `a = makeHashMap();`

Post: `a` now contains a new empty `ConcurrentHashMap` Object.

makeObject

Use: `obj = makeObject(con, args);`

Pre: `con` must be a constructor, as returned from the function `findConstructor`, `args` is a list of arguments appropriate for the constructor.

Post: `obj` contains a reference to a newly created object constructed using the constructor with the given arguments.

makeReady

Use: `makeReady(f);`

Pre: `f` must be a fiber state associated with a fiber that is currently not running.

Post: The fiber associated with `f` is now running, i.e. it will receive control once in a while when other fibers in the same task release control of the task.

makeUnique

Use: `c = makeUnique();`

Post: `c` now contains a new object (a `java.lang.Object` object).

memoize

Use: `g = memoize(f);`

Pre: `f` is a function that takes no argument.

Post: `g` is a function that takes no argument. When `g` is called for the first time it calls `f` and returns the value returned by `f`. Subsequent times when `g` is called it returns that same value without calling `f`.

nanoTime

Use: `t = nanoTime();`

Post: `t` contains a `Long` value that is a count of nanoseconds from some starting time, same as the static function `nanoTime` in the Java class `java.lang.System`.

printExceptionTrace

Use: `printExceptionTrace(e);`

Pre: `e` is an exception caught in a **catch** part of a try-catch expression. The call to `printExceptionTrace` must be inside the catch part of the expression.

Post: A trace of the exception has been written to standard output.

printExceptionTrace

Use: `printExceptionTrace();`

Pre: The call is inside a **catch** part of a try-catch expression.

Post: A trace of the exception has been written to standard output.

random

Use: `x = random(n);`

Pre: `n` is an integer, greater than zero.

Post: `x` is a random integer value, $0 \leq x < n$.

readLine

Use: `x = readLine();`

Post: The next input line has been read from standard input and `x` contains the line as a string value.

scanner

Use: `s = scanner();`

Post: `s` refers to a scanner (`java.util.Scanner`) that is connected to standard input.

setHead

Use: `setHead(x,y);`

Pre: `x` is a pair, `y` can be any value.

Post: The head of the pair `x` has been set to `y`.

setTail

Use: `setTail(x,y);`

Pre: `x` is a pair, `y` can be any value.

Post: The tail of the pair `x` has been set to `y`.

short

Use: `y = short(x);`

Pre: `x` must be `BigInteger`, `Long`, `Integer`, `Short`, `Character` or `Byte`.

Post: `y` now contains the same value (if possible), but as a `Short` object.

sin

Use: `y = sin(r);`

Pre: `r` is a `Double` value denoting an angle in radians.

Post: `y` now contains the sine of `r`.

sleep

Use: `sleep(d);`

Pre: `d` is either a Double value denoting an interval in seconds or an integer value denoting an interval in nanoseconds.

Post: The current fiber has slept for the given interval.

sqrt

Use: `y = sqrt(x);`

Pre: `x` is a non-negative Double value.

Post: `y` now contains the square root of `x`.

startBackgroundTask

Use: `startBackgroundTask(f);|`

Pre: `f` must be a function (a closure) taking no argument.

Post: A new background task has been started in a special background machine that has multiple threads. The task executes the given function and then terminates.

startBackgroundTask

Use: `startBackgroundTask(f,x);|`

Pre: `f` must be a function (a closure) taking one argument, `x` must be a valid argument to the function.

Post: A new background task has been started in a special background machine that has multiple threads. The task executes the given function with the given argument and then terminates.

startFiber

Use: `startFiber(f);|`

Pre: `f` must be a function (a closure) taking no argument.

Post: A new fiber has been started in the current task. The fiber executes the given function and then terminates.

startFiber

Use: startFiber(f,x);|

Pre: f must be a function (a closure) taking one argument, x must be a valid argument to the function.

Post: A new fiber has been started in the current task. The fiber executes the given function with the given argument and then terminates.

startForegroundTask

Use: startForegroundTask(f);|

Pre: f must be a function (a closure) taking no argument.

Post: A new foreground task has been started in the special foreground machine that has a single thread. The task executes the given function and then terminates.

startForegroundTask

Use: startForegroundTask(f,x);|

Pre: f must be a function (a closure) taking one argument, x must be a valid argument to the function.

Post: A new foreground task has been started in the special foreground machine that has a single thread. The task executes the given function with the given argument and then terminates.

startMachine

Use: startMachine(f);|

Pre: f must be a function (a closure) taking no argument.

Post: A new machine has been started. The machine executes the given function and then terminates.

startMachine

Use: `startMachine(f,x);`

Pre: f must be a function (a closure) taking one argument, x must be a valid argument to the function.

Post: A new machine has been started. The machine executes the given function with the given argument and then terminates.

startTask

Use: `startTask(f);`

Pre: f must be a function (a closure) taking no argument.

Post: A new task has been started in the current machine. The task executes the given function and then terminates.

startTask

Use: `startTask(f,x);`

Pre: f must be a function (a closure) taking one argument, x must be a valid argument to the function.

Post: A new task has been started in the current machine. The task executes the given function with the given argument and then terminates.

streamAppend

Use: `z = streamAppend(x,y);`

Pre: x and y are streams.

Post: z is a stream that contains the values in x followed by the values in y .

streamConcatMap

Use: `y = streamConcatMap(f,x);`

Pre: x is a stream, f is a function of one argument that returns a stream.

Post: y is the stream of values resulting from concatenating the streams resulting from applying f to all the the values in x in sequence. See also `>>=`.

streamConcat

Use: `y = streamConcat(x);`

Pre: `x` is a stream of streams.

Post: `y` is the stream of values resulting when all the streams in `x` are concatenated.

streamHead

Use: `y = streamHead(x);`

Pre: `x` is a non-empty stream.

Post: `y` is the head of the stream `x`.

streamMap

Use: `y = streamMap(f, x);`

Pre: `x` is a stream, `f` is a function of one argument.

Post: `y` is the stream of values resulting when `f` is applied to all the values in `x`.

streamTail

Use: `y = streamTail(x);`

Pre: `x` must be a non-empty stream.

Post: `y` is the tail of `x`.

Example: The code

```
1 {  
2   rec val e = #[ 1 $ e ];  
3   writeln(streamHead(streamTail(e)));  
4 }
```

will write the number 1.

streamToList

Use: `y = streamToList(x);`

Pre: `x` is a finite stream.

Post: `y` is the list of values in `x`.

suspend

Use: `suspend();`

Post: There is no actual postcondition since the current fiber has been suspended until perhaps some other fiber somehow resumes it (using, for example, the transfer BASIS function). In the case of resumption, the current fiber will in any case resume from some other (previously saved) point of control.

tail

Use: `y = tail(x);`

Pre: `x` is a pair.

Post: `y` is the tail of `x`.

tan

Use: `y = tan(r);`

Pre: `r` is a Double denoting an angle in radians.

Post: `y` is the tangent of `r`.

transfer

Use: `y = transfer(from, to, x);`

Pre: The last argument, `x`, can be any value. There are three possible valid cases for the other arguments:

1. `from` may be null and `to` may be a fiber state (an `is.hi.cs.morpho.FiberState` object) that has previously received initialization by being a first argument in a call to `transfer`. The fiber state object must have been previously created in the current task.

2. `from` may be a fiber state (an `is.hi.cs.morpho.FiberState` object) and `to` may be null. The fiber state in `from` must have been created in the current task.
3. Both `from` and `to` may be fiber states (`is.hi.cs.morpho.FiberState` objects) and `to` has previously received initialization by being a first argument in a call to `transfer`. Both fiber states must have been created in the current task.

Post: The results for the three different cases are:

1. The current fiber is suspended and control passes to the fiber denoted by `to`. The fiber denoted by `to` will resume from the previously executed call to `transfer` in that fiber, and that call will return `x` as its value.
2. The current fiber continues just as if nothing had happened, and `y` now contains `x`. However, `from` now contains a fiber state that allows a later transfer to the exact same point of control, using a later call to `transfer`.
3. In the case where both `from` and `to` are fiber states (`is.hi.cs.morpho.FiberState` objects), the current fiber is suspended, but its state is saved in `from`, so it can be resumed later using a later call to `transfer`. Control passes to the fiber denoted by `to`, to the call to `transfer` that initialized `to`. The value returned by that call is `x`.

Note: This is a very powerful and primitive function that should only be used when absolutely necessary when other methods of flow control, including the exception handling functionality, are not powerful enough. The interaction of this functionality with exception handling and global variable functionality is a bit tricky.

turtle

Use: `t = turtle();`

Post: A new graphics window has been created and made visible on the screen. The value `t` refers to a new turtle object that can be used to draw upon the graphics window. Originally the graphics window has a coordinate system with x and y ranging from -1.0 to 1.0 , with the bottom-left corner at $(-1, -1)$. The turtle is originally located at $(0, 0)$ with a direction to the left, i.e. an angle of 0 radians. The turtle referred to by `t` responds to the following messages:

forward

Use: `t.forward(d);`

Pre: `t` is a turtle, `d` is a Double value.

Post: The turtle has been moved a distance of `d` in its current direction, and if it is down then a line has been drawn with the current color from the old position to the new position.

left

Use: `t.left();`

Pre: `t` is a turtle.

Post: The turtle has been turned 90 degrees ($\pi/2$ radians) to the left.

right

Use: `t.right();`

Pre: `t` is a turtle.

Post: The turtle has been turned 90 degrees ($\pi/2$ radians) to the right.

turn

Use: `t.turn(a);`

Pre: `t` is a turtle, `a` is a Double value.

Post: The turtle has been turned `a` radians to the left.

color

Use: `t.color(r,g,b);`

Pre: `t` is a turtle, `r`, `g`, and `b` are integer values, $0 \leq r, g, b < 256$.

Post: The color of the turtle has been set to the color denoted by the integer values, where `r`, `g`, and `b` stand for red, green and blue intensities, respectively.

hide

Use: `t.hide();`

Pre: `t` is a turtle.

Post: The turtle has been hidden and will not be visible on the graphics window.

show

Use: `t.show()`;

Pre: `t` is a turtle.

Post: The turtle has been shown and will be visible on the graphics window.

up

Use: `t.up()`;

Pre: `t` is a turtle.

Post: The pen of the turtle has been lifted and will not draw on the graphics window.

down

Use: `t.down()`;

Pre: `t` is a turtle.

Post: The pen of the turtle has been put down and will draw on the graphics window.

set direction

Use: `t.direction(a)`;

Pre: `t` is a turtle, `a` is a Double value.

Post: The turtle has been turned so that it points `a` radians to the left of the x-axis.

moveTo

Use: `t.moveTo(x,y)`;

Pre: `t` is a turtle, `x` and `y` are Double values.

Post: The turtle has been moved to `(x,y)` without drawing anything.

drawTo

Use: `t.moveTo(x,y)`;

Pre: `t` is a turtle, `x` and `y` are Double values.

Post: The turtle has been moved to `(x,y)` and has drawn a line from the old position to the new one using the current color.

x position

Use: `z = t.x`;

Pre: `t` is a turtle.

Post: `z` contains the x-position of the turtle.

y position

Use: `z = t.y;`

Pre: `t` is a turtle.

Post: `z` contains the y-position of the turtle.

angle

Use: `a = t.angle;`

Pre: `t` is a turtle.

Post: `a` contains the angle of the turtle.

hidden

Use: `h = t.hidden;`

Pre: `t` is a turtle.

Post: `h` contains true iff the turtle is hidden.

up

Use: `u = t.up;`

Pre: `t` is a turtle.

Post: `u` contains true iff the turtle's pen is lifted.

Set Scaling

Use: `t.setScaling(xorg,yorg,xscale,yscale);`

Pre: `t` is a turtle, `xorg`, `yorg`, `xscale`, and `yscale` are Double values.

Post: The scaling transformation of the turtle has been set to the given values. `xorg` is the x coordinate in the graphics window that the point (0,0) maps to, `yorg` is the y coordinate in the graphics window that the point (0,0) maps to, `xscale` is the scale multiplier in the x-direction, and `yscale` is the scale multiplier in the x-direction. This means in general that a turtle coordinate (x,y) will map to the coordinate (xorg+x*xscale,yorg+y*yscale).

The original scaling of the turtle for a newly created graphics window is

- `xorg = 250.0`
- `yorg = 250.0`
- `xscale = 250.0`
- `yscale = -250.0`

x origin

Use: `xorg = t.xorg`

Pre: `t` is a turtle.

Post: `xorg` is the x origin of the turtle, see the `setScaling` message II on the preceding page.

y origin

Use: `yorg = t.yorg`

Pre: `t` is a turtle.

Post: `yorg` is the y origin of the turtle, see the `setScaling` message II on the previous page.

x scale

Use: `xscale = t.xscale`

Pre: `t` is a turtle.

Post: `xscale` is the x scale of the turtle, see the `setScaling` message II on the preceding page.

y scale

Use: `yscale = t.yscale`

Pre: `t` is a turtle.

Post: `yscale` is the y scale of the turtle, see the `setScaling` message II on the previous page.

width

Use: `w = t.width`

Pre: `t` is a turtle.

Post: `w` is the width of the content area of the graphics window containing the turtle.

height

Use: `h = t.width`

Pre: `t` is a turtle.

Post: `h` is the height of the content area of the graphics window containing the turtle.

setSize

Use: `t.setSize(w,h)`

Pre: `t` is a turtle, `w` and `h` are Double values.

Post: The width and height of the content area of the graphics window containing the turtle have been set to the values given.

window

Use: `w = t.window`

Pre: `t` is a turtle.

Post: `w` refers to the Java object that stands for the graphics window containing the turtle.

write

Use: `write(x);`

Pre: `x` is any value.

Post: A text representation of `x` has been written to standard output.

writeln

Use: `writeln();`

Post: A newline has been written to standard output.

writeln

Use: `writeln(x);`

Pre: `x` is any value.

Post: A text representation of `x` and a subsequent newline has been written to standard output.

yield**Use:** `yield();`**Post:** The current fiber has yielded control temporarily to other fibers in the same task. Once control is yielded or transferred back, this call returns.

Part III

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